

# Semantic Segmentation of 3D point Clouds

Loïc Landrieu

Université Paris-Est - Machine Learning and  
Optimization working Group

March 2019

# Presentation

---

- Loic Landrieu, researcher at IGN (French Mapping Agency) in the AI department

## Presentation

---

- Loic Landrieu, researcher at IGN (French Mapping Agency) in the AI department
- PhD at INRIA/ENPC on *Graph-Structured Learning and Optimization*, w. Francis Bach and Guillaume Obozinski

## Presentation

---

- Loic Landrieu, researcher at IGN (French Mapping Agency) in the AI department
- PhD at INRIA/ENPC on *Graph-Structured Learning and Optimization*, w. Francis Bach and Guillaume Obozinski
- **Interest:** graph-structured functional optimization and deep learning.

# Presentation

---

- Loic Landrieu, researcher at IGN (French Mapping Agency) in the AI department
- PhD at INRIA/ENPC on *Graph-Structured Learning and Optimization*, w. Francis Bach and Guillaume Obozinski
- **Interest:** graph-structured functional optimization and deep learning.
- **Applications:** 3D point clouds, dynamic 3D for autonomous driving, superspectral satellite images, time series, medical inverse problems.

## Presentation outline

---

- 1 Deep Learning for 3D Point Clouds
- 2 Learning 3D Point Clouds Segmentation
- 3 The Cut Pursuit Algorithm
- 4 Conclusion
- 5 Bibliography

# Presentation Layout

---

- 1 Deep Learning for 3D Point Clouds
- 2 Learning 3D Point Clouds Segmentation
- 3 The Cut Pursuit Algorithm
- 4 Conclusion
- 5 Bibliography

# Presentation Layout

---

- 1 **Deep Learning for 3D Point Clouds**
  - Presentation of the Problem
  - Traditional Approaches
  - First Deep-Learning Approaches
  - Scaling Segmentation
- 2 **Learning 3D Point Clouds Segmentation**
- 3 **The Cut Pursuit Algorithm**
- 4 **Conclusion**
- 5 **Bibliography**

## Capturing a 3D world

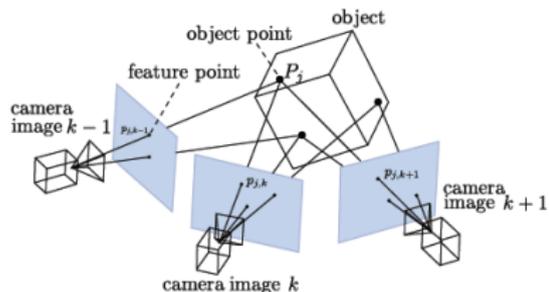
- 3D data crucial for robotics, autonomous vehicle, 3D scale models, virtual reality etc...



**credit:** medium, VisionSystemDesign, microsoft

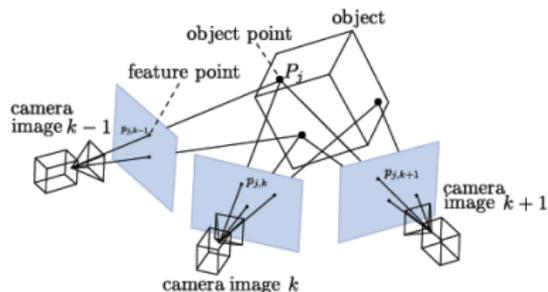
## Capturing a 3D world

- 3D data crucial for robotics, autonomous vehicle, 3D scale models, virtual reality etc...
- Can be computed from images: stereo, SfM, SLAM (cheap, not precise).



# Capturing a 3D world

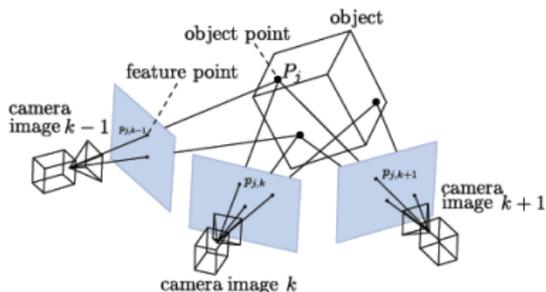
- 3D data crucial for robotics, autonomous vehicle, 3D scale models, virtual reality etc...
- Can be computed from images: stereo, SfM, SLAM (cheap, not precise).
- LiDAR (expensive, precise).



credit: computervisionblog, velodynelidar

# Capturing a 3D world

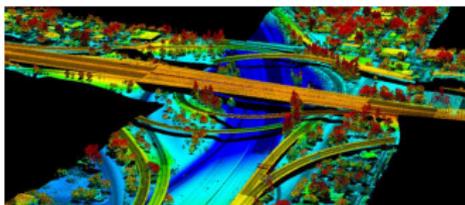
- 3D data crucial for robotics, autonomous vehicle, 3D scale models, virtual reality etc...
- Can be computed from images: stereo, SfM, SLAM (cheap, not precise).
- LiDAR (expensive, precise).
- Can be fixed, mobile, aerial, drone-embarked.



credit: computervisionblog, velodynelidar

# Capturing a 3D world

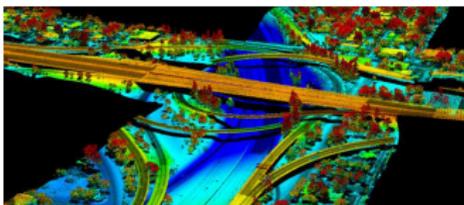
- 3D data crucial for robotics, autonomous vehicle, 3D scale models, virtual reality etc...
- Can be computed from images: stereo, SfM, SLAM (cheap, not precise).
- LiDAR (expensive, precise).
- Can be fixed, mobile, aerial, drone-embarked.
- Produces a 3D point cloud:  
 $P \in \mathbb{R}^{n \times 3}$ .



credit: clearpath robotics, tuck mapping solutions

# Capturing a 3D world

- 3D data crucial for robotics, autonomous vehicle, 3D scale models, virtual reality etc...
- Can be computed from images: stereo, SfM, SLAM (cheap, not precise).
- LiDAR (expensive, precise).
- Can be fixed, mobile, aerial, drone-embarked.
- Produces a 3D point cloud:  
 $P \in \mathbb{R}^{n \times 3}$ .
- Large acquisition:  $n$  typically in the  $10^8$ s.



credit: clearpath robotics, tuck mapping solutions

## Future trends

---

- LiDAR are getting cheaper :100k\$ → 2k\$ in a few years.

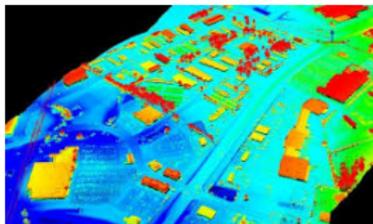


**credit:** velodynelidar, green car congress

## Future trends

---

- LiDAR are getting cheaper :100k\$ → 2k\$ in a few years.
- Also coming: solid state LiDAR (cheap, fast and resilient), single photon LiDAR (unmatched acquisition density).

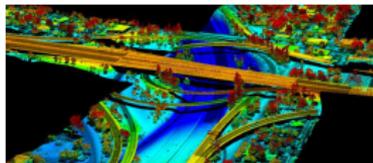


credit: velodynelidar, spar3d

## Future trends

---

- LiDAR are getting cheaper :100k\$ → 2k\$ in a few years.
- Also coming: solid state LiDAR (cheap, fast and resilient), single photon LiDAR (unmatched acquisition density).
- **Major industrial application:** autonomous driving, virtual models, land surveyy...

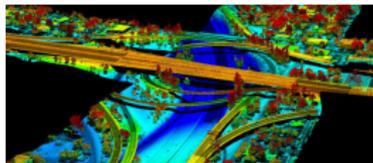


**credit:** tuck mapping solutions, clearpath robotics

## Future trends

---

- LiDAR are getting cheaper :100k\$ → 2k\$ in a few years.
- Also coming: solid state LiDAR (cheap, fast and resilient), single photon LiDAR (unmatched acquisition density).
- **Major industrial application:** autonomous driving, virtual models, land surveyy...
- **Also to come:** major advances in automatic analysis of 3D data.

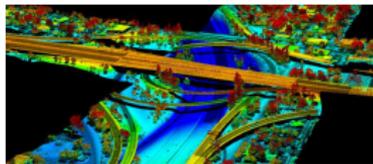


**credit:** tuck mapping solutions, clearpath robotics

## Future trends

---

- LiDAR are getting cheaper :100k\$ → 2k\$ in a few years.
- Also coming: solid state LiDAR (cheap, fast and resilient), single photon LiDAR (unmatched acquisition density).
- **Major industrial application:** autonomous driving, virtual models, land surveyy...
- **Also to come:** major advances in automatic analysis of 3D data.
- Rapid progress in hardware and methodology + major applications = a **booming field**.

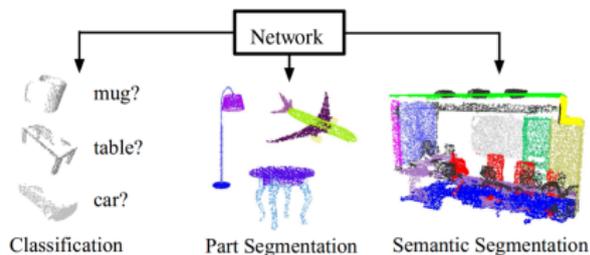


**credit:** tuck mapping solutions, clearpath robotics

# Analysis of 3D point clouds

- **Classification:** classify the point cloud among class set  $\mathcal{K}$ :

$$P \mapsto \mathcal{K}$$



credit: Qi et. al. 2017a

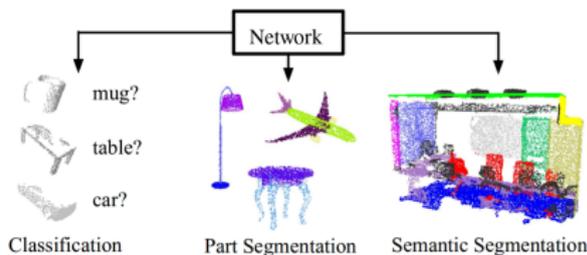
# Analysis of 3D point clouds

- **Classification:** classify the point cloud among class set  $\mathcal{K}$ :

$$P \mapsto \mathcal{K}$$

- **Partition:** cluster the point cloud in  $C$  parts/object:

$$P_i \mapsto [1, \dots, C]$$



credit: Qi et. al. 2017a

# Analysis of 3D point clouds

- **Classification:** classify the point cloud among class set  $\mathcal{K}$ :

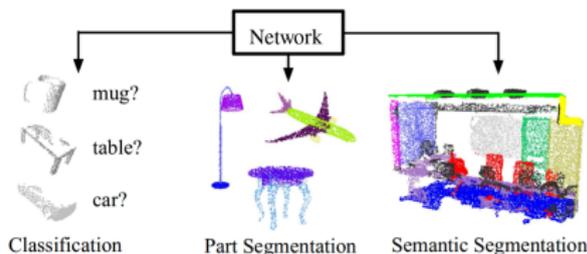
$$P \mapsto \mathcal{K}$$

- **Partition:** cluster the point cloud in  $C$  parts/object:

$$P_i \mapsto [1, \dots, C]$$

- **Semantic Segmentation:** classify each point of a point cloud between  $K$  classes:

$$P_i \mapsto [1, \dots, K]$$



credit: Qi et. al. 2017a

# Analysis of 3D point clouds

- **Classification:** classify the point cloud among class set  $\mathcal{K}$ :

$$P \mapsto \mathcal{K}$$

- **Partition:** cluster the point cloud in  $C$  parts/object:

$$P_i \mapsto [1, \dots, C]$$

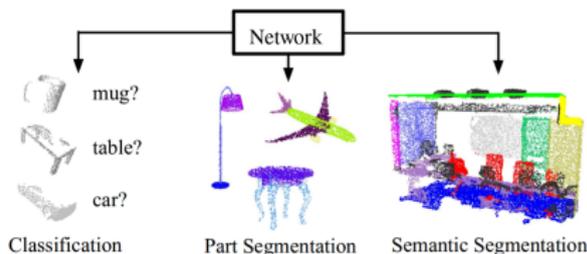
- **Semantic Segmentation:** classify each point of a point cloud between  $K$  classes:

$$P_i \mapsto [1, \dots, K]$$

- **Instance Segmentation:** cluster the point cloud into semantically characterized objects:

$$P_i \mapsto [1, \dots, C]$$

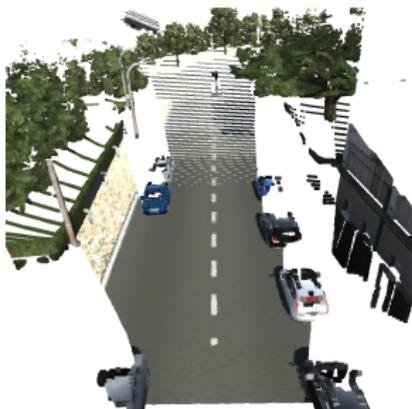
$$[1, \dots, C] \mapsto [1, \dots, K]$$



# What makes 3D analysis so hard

---

- Data volume considerable.

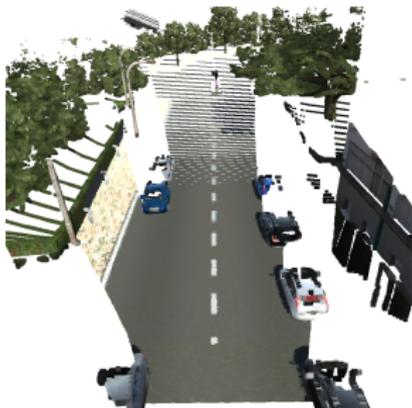


credit: Gaidon2016, Engelmann2017, Hackel2017

# What makes 3D analysis so hard

---

- Data volume considerable.
- Lack of grid-structure.

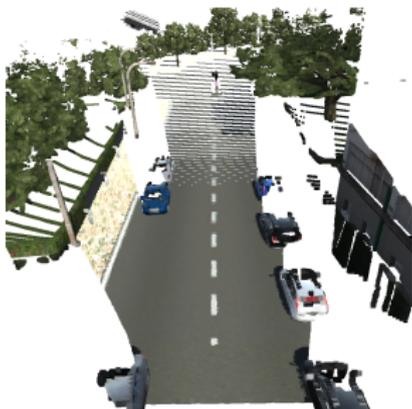


credit: Gaidon2016, Engelmann2017, Hackel2017

# What makes 3D analysis so hard

---

- Data volume considerable.
- Lack of grid-structure.
- Permutation-invariance.

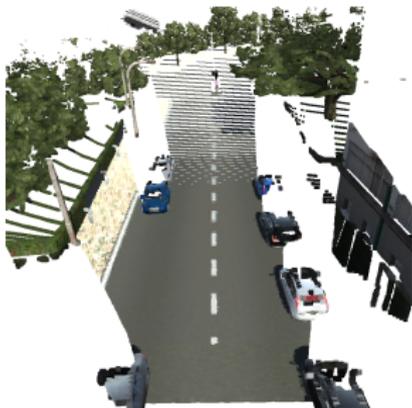


credit: Gaidon2016, Engelmann2017, Hackel2017

# What makes 3D analysis so hard

---

- Data volume considerable.
- Lack of grid-structure.
- Permutation-invariance.
- Sparsity.

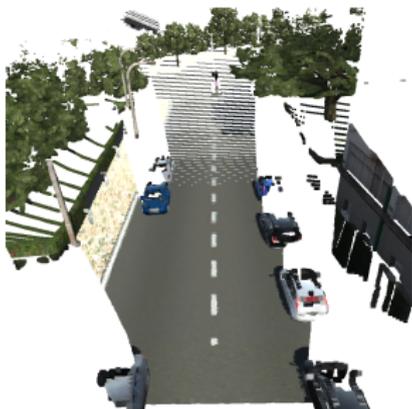


credit: Gaidon2016, Engelmann2017, Hackel2017

# What makes 3D analysis so hard

---

- Data volume considerable.
- Lack of grid-structure.
- Permutation-invariance.
- Sparsity.
- Highly variable density.

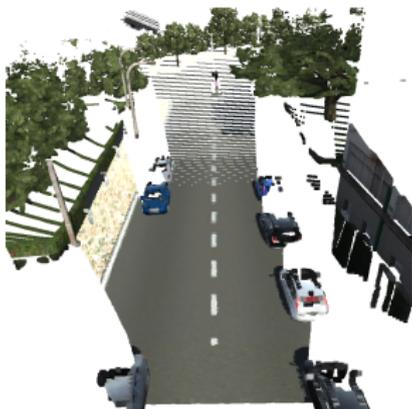


credit: Gaidon2016, Engelmann2017, Hackel2017

# What makes 3D analysis so hard

---

- Data volume considerable.
- Lack of grid-structure.
- Permutation-invariance.
- Sparsity.
- Highly variable density.
- Acquisition artifacts.

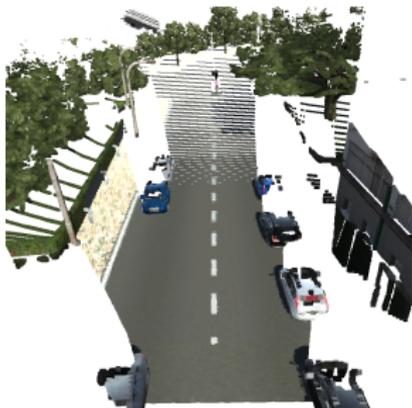


credit: Gaidon2016, Engelmann2017, Hackel2017

# What makes 3D analysis so hard

---

- Data volume considerable.
- Lack of grid-structure.
- Permutation-invariance.
- Sparsity.
- Highly variable density.
- Acquisition artifacts.
- Occlusions.



credit: Gaidon2016, Engelmann2017, Hackel2017

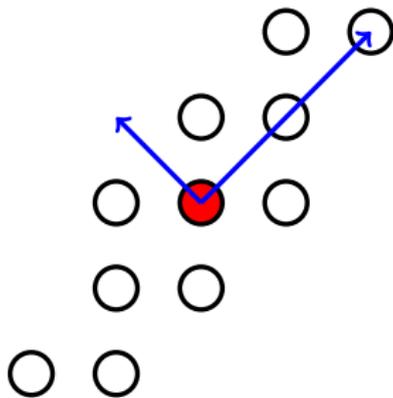
# Presentation Layout

---

- 1 **Deep Learning for 3D Point Clouds**
  - Presentation of the Problem
  - Traditional Approaches
  - First Deep-Learning Approaches
  - Scaling Segmentation
- 2 **Learning 3D Point Clouds Segmentation**
- 3 **The Cut Pursuit Algorithm**
- 4 **Conclusion**
- 5 **Bibliography**

## Pointwise classification

- **Step 1:** compute point features based on neighborhood



$$Lin = \frac{\sqrt{\lambda_1} - \sqrt{\lambda_2}}{\sqrt{\lambda_1}}$$

$$Pla = \frac{\sqrt{\lambda_2} - \sqrt{\lambda_3}}{\sqrt{\lambda_1}}$$

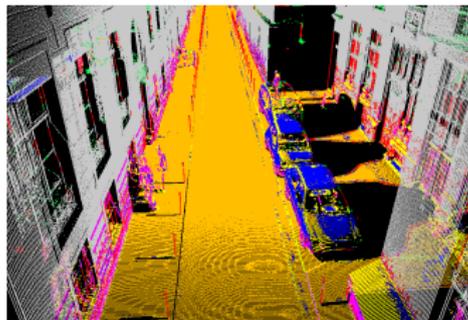
$$Sca = \frac{\sqrt{\lambda_3}}{\sqrt{\lambda_1}}$$

Demantke2011

## Pointwise classification

---

- **Step 1:** compute point features based on neighborhood
- **Step 2:** classification (RF, SVM, etc...)

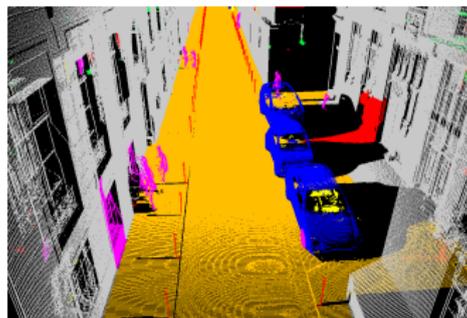
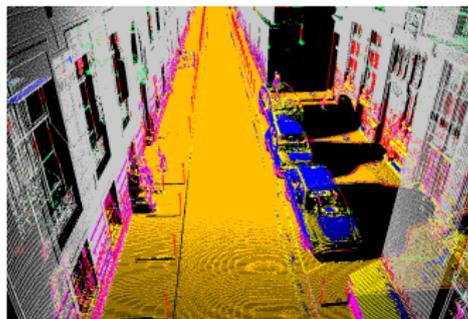


Demantke2011  
Weimann2015

**credit:** landrieu et. al. 2017a

## Pointwise classification

- **Step 1:** compute point features based on neighborhood
- **Step 2:** classification (RF, SVM, etc...)
- **Step 3:** smoothing to increase spatial regularity (with CRFs, MRFs, graph-structured optimization, etc...)



Demantke2011  
Weimann2015  
Landrieu et. al. 2017a

credit: landrieu et. al. 2017a

# Presentation Layout

---

- 1 **Deep Learning for 3D Point Clouds**
  - Presentation of the Problem
  - Traditional Approaches
  - First Deep-Learning Approaches
  - Scaling Segmentation
- 2 **Learning 3D Point Clouds Segmentation**
- 3 **The Cut Pursuit Algorithm**
- 4 **Conclusion**
- 5 **Bibliography**

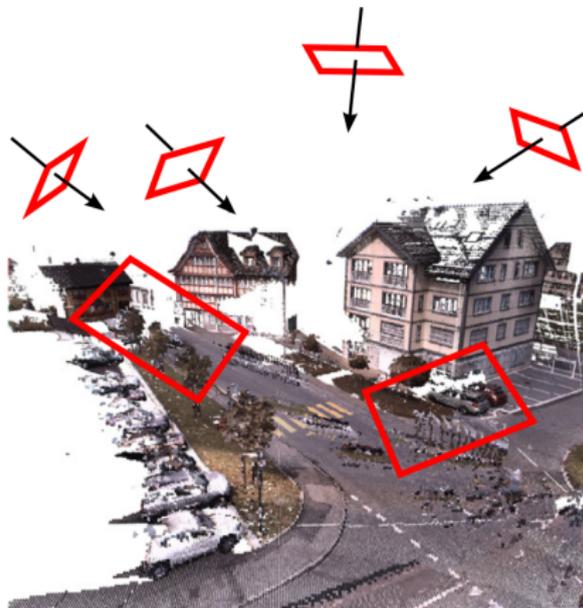
## Image-Based Methods

---

- **A simple observation:** CNNs works great for images. Can we use images for 3D?

## Image-Based Methods

- **A simple observation:** CNNs works great for images. Can we use images for 3D?
- **SnapNet:**



Boulch et. al. 2017

credit: Boulch et. al. 2017

## Image-Based Methods

- **A simple observation:** CNNs works great for images. Can we use images for 3D?
- **SnapNet:**
  - surface reconstruction



Boulch et. al. 2017

credit: Boulch et. al. 2017

## Image-Based Methods

- **A simple observation:** CNNs works great for images. Can we use images for 3D?
- **SnapNet:**
  - surface reconstruction
  - *virtual snapshots*



Boulch et. al. 2017

credit: Boulch et. al. 2017

## Image-Based Methods

- **A simple observation:** CNNs works great for images. Can we use images for 3D?
- **SnapNet:**
  - surface reconstruction
  - *virtual snapshots*
  - semantic segmentation of resulting images with CNNs



Boulch et. al. 2017

credit: Boulch et. al. 2017

## Image-Based Methods

- **A simple observation:** CNNs works great for images. Can we use images for 3D?
- **SnapNet:**
  - surface reconstruction
  - *virtual snapshots*
  - semantic segmentation of resulting images with CNNs
  - project prediction back to p.c.



Boulch et. al. 2017

credit: Boulch et. al. 2017

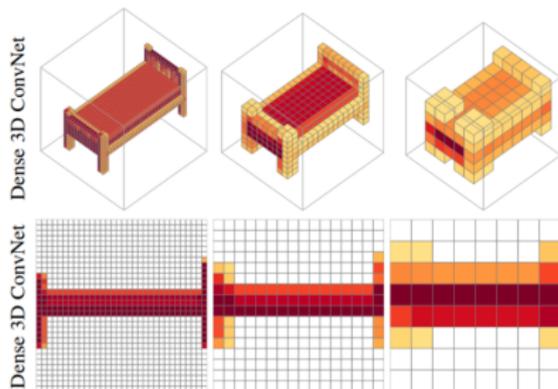
## Voxel-Based Methods

---

- **Idea:** generalize 2D convolutions to regular 3D grids

## Voxel-Based Methods

- **Idea:** generalize 2D convolutions to regular 3D grids
- Voxelization + 3D convNets

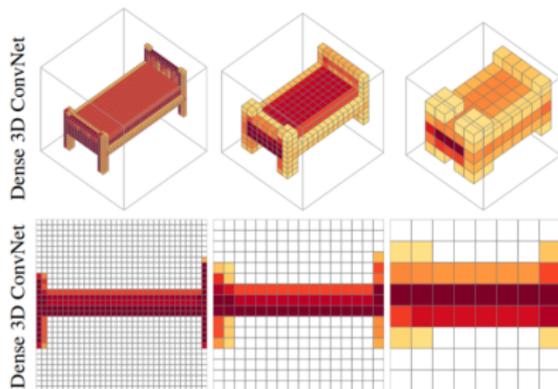


Wu2015

credit: Riegler2017, Tchapmi2017, Jampani2017

## Voxel-Based Methods

- **Idea:** generalize 2D convolutions to regular 3D grids
- Voxelization + 3D convNets
- **Problem:** inefficient representation, loss of invariance, costly (cubic)

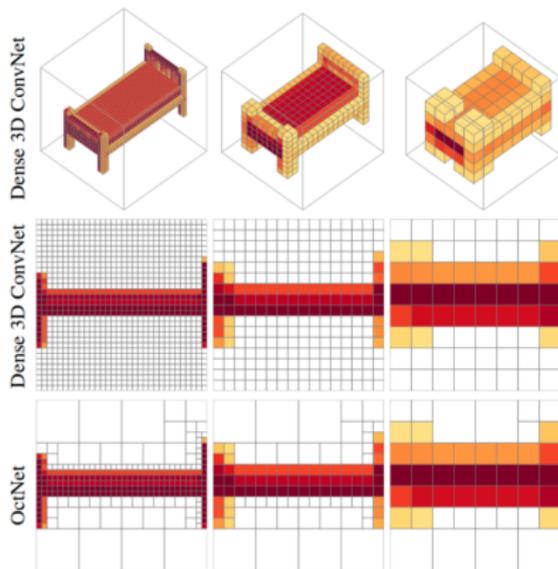


Wu2015

credit: Riegler2017, Tchapmi2017, Jampani2017

## Voxel-Based Methods

- **Idea:** generalize 2D convolutions to regular 3D grids
- Voxelization + 3D convNets
- **Problem:** inefficient representation, loss of invariance, costly (cubic)
- **Idea 1:** OctNet, OctTree based approach

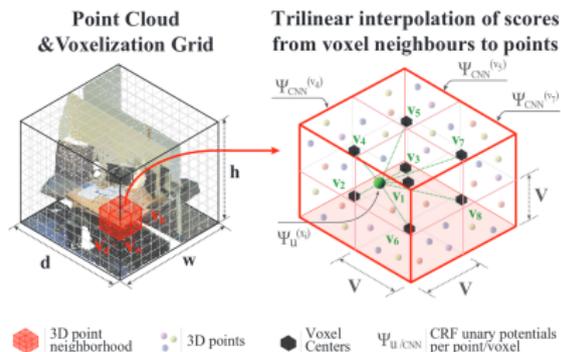


Wu2015 , Riegler2017

credit: Riegler2017, Tchapmi2017, Jampani2017

## Voxel-Based Methods

- **Idea:** generalize 2D convolutions to regular 3D grids
- Voxelization + 3D convNets
- **Problem:** inefficient representation, loss of invariance, costly (cubic)
- **Idea 1:** OctNet, OctTree based approach
- **Idea 2:** SegCloud, large voxels, subvoxel predictions with CRFs.

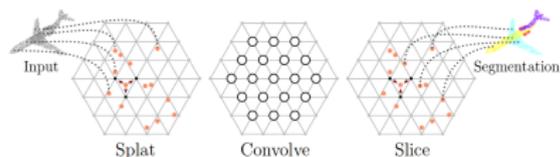


Wu2015 , Riegler2017 , Tchapmi2017, Jampani2018.

credit: Riegler2017, Tchapmi2017, Jampani2017

## Voxel-Based Methods

- **Idea:** generalize 2D convolutions to regular 3D grids
- Voxelization + 3D convNets
- **Problem:** inefficient representation, loss of invariance, costly (cubic)
- **Idea 1:** OctNet, OctTree based approach
- **Idea 2:** SegCloud, large voxels, subvoxel predictions with CRFs.
- **Idea 3:** SplatNet, sparse convolutions with hashmaps.



Wu2015 , Riegler2017 , Tchapmi2017, Jampani2018.

**credit:** Riegler2017, Tchapmi2017, Jampani2017

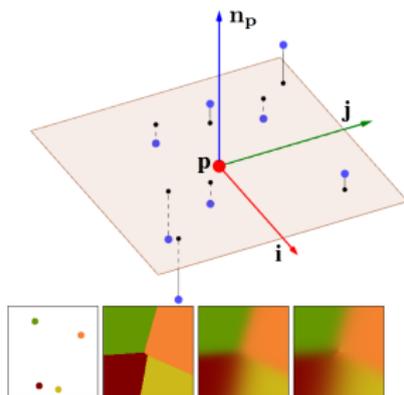
## 3D Convolution-Based Methods

---

- **Idea:** generalize 2D convolutions to 3D point clouds as unordered data.

## 3D Convolution-Based Methods

- **Idea:** generalize 2D convolutions to 3D point clouds as unordered data.
- **Tangent Convolution:** 2D convolution in the tangent space of each point.

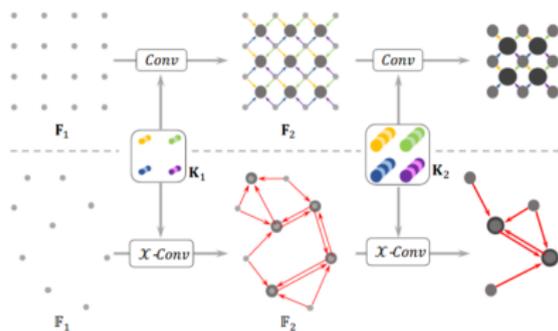


Tatarchenko2018

credit: Tatarchenko2018, Li2018

## 3D Convolution-Based Methods

- **Idea:** generalize 2D convolutions to 3D point clouds as unordered data.
- **Tangent Convolution:** 2D convolution in the tangent space of each point.
- **PointCNN** :  $\chi$ -convolutions: generalized convolutions for unordered inputs.

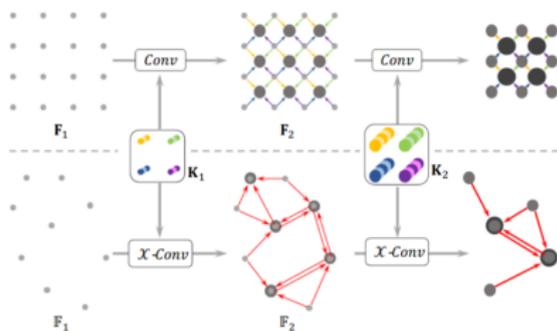


Tatarchenko2018 , Li2018.

credit: Tatarchenko2018, Li2018

## 3D Convolution-Based Methods

- **Idea:** generalize 2D convolutions to 3D point clouds as unordered data.
- **Tangent Convolution:** 2D convolution in the tangent space of each point.
- **PointCNN** :  $\chi$ -convolutions: generalized convolutions for unordered inputs.
- **Principle:** the network learns how to permute *ordered* inputs

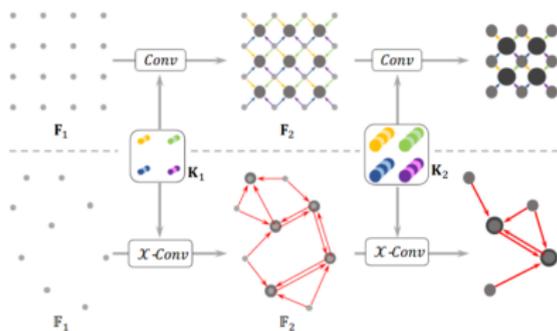


Tatarchenko2018 , Li2018.

credit: Tatarchenko2018, Li2018

## 3D Convolution-Based Methods

- **Idea:** generalize 2D convolutions to 3D point clouds as unordered data.
- **Tangent Convolution:** 2D convolution in the tangent space of each point.
- **PointCNN** :  $\chi$ -convolutions: generalized convolutions for unordered inputs.
- **Principle:** the network learns how to permute *ordered* inputs
- The invariance is learnt!



Tatarchenko2018 , Li2018.

credit: Tatarchenko2018, Li2018

# PointNet

---

- **A fundamental constraint:** inputs are invariant by permutation

Qi et. al.2017a

# PointNet

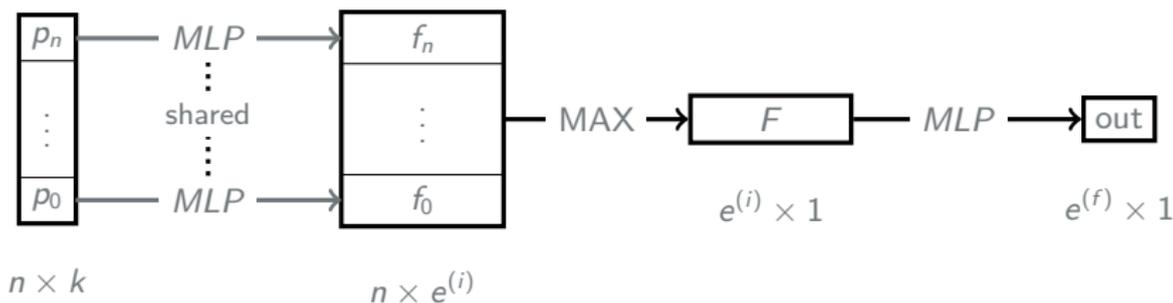
---

- **A fundamental constraint:** inputs are invariant by permutation
- **Solution:** process points independently, apply permutation-invariant pooling, process this feature with a MLP.

Qi et. al.2017a

# PointNet

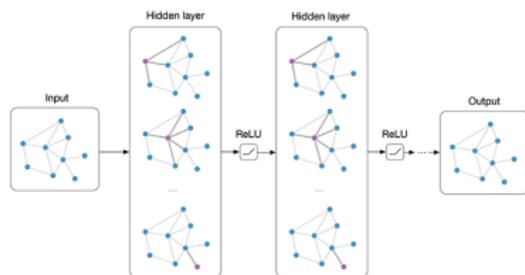
- **A fundamental constraint:** inputs are invariant by permutation
- **Solution:** process points independently, apply permutation-invariant pooling, process this feature with a MLP.
- $n$ : number of points,  $k$  size of observations,  $e^{(i)}$  size of intermediary embeddings,  $e^{(f)}$  size of output



Qi et. al.2017a

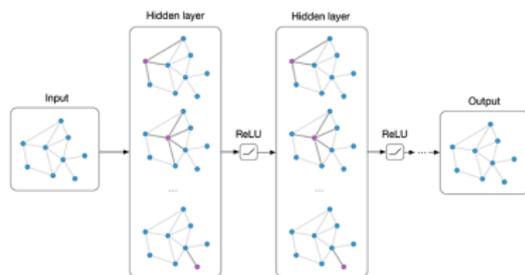
# Graph-Neural Network

- Generalize convolutions to the general graph setting.



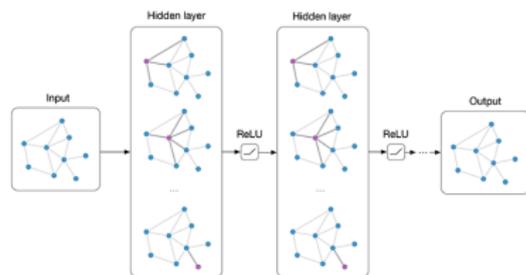
# Graph-Neural Network

- Generalize convolutions to the general graph setting.
- For example: k-nearest neighbors graph of 3D points.



# Graph-Neural Network

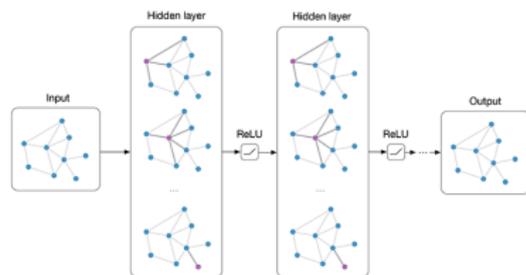
- Generalize convolutions to the general graph setting.
- For example: k-nearest neighbors graph of 3D points.
- **Idea:** Each point maintain a hidden state  $h_i$  influenced by its neighbors.



# Graph-Neural Network

- Generalize convolutions to the general graph setting.
- For example: k-nearest neighbors graph of 3D points.
- **Idea:** Each point maintain a hidden state  $h_i$  influenced by its neighbors.
- **GNN Qi2017:** an iterative message-passing algorithm using a mapping  $f$  and a RNN  $g$ :

$$h_i^{(t+1)} = g\left(\sum_{j \rightarrow i} f(h_i^t, h_j^t)\right)$$



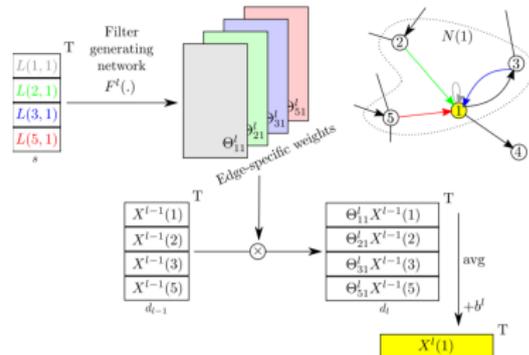
# Graph-Neural Network

- Generalize convolutions to the general graph setting.
- For example: k-nearest neighbors graph of 3D points.
- **Idea:** Each point maintain a hidden state  $h_i$  influenced by its neighbors.
- **GNN Qi2017:** an iterative message-passing algorithm using a mapping  $f$  and a RNN  $g$ :

$$h_i^{(t+1)} = g\left(\sum_{j \rightarrow i} f(h_j^t, h_i^t)\right)$$

- **ECC Simonovski2017** messages are conditioned by edge features:

$$h_i^{(t+1)} = g\left(\sum_{j \rightarrow i} \Theta_{i,j} \odot h_j^t, h_i^t\right)$$



Qi2017, Simonovski2017

credit: Simonovski2017

# Presentation Layout

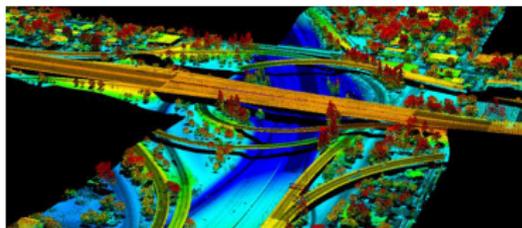
---

- 1 **Deep Learning for 3D Point Clouds**
  - Presentation of the Problem
  - Traditional Approaches
  - First Deep-Learning Approaches
  - **Scaling Segmentation**
- 2 **Learning 3D Point Clouds Segmentation**
- 3 **The Cut Pursuit Algorithm**
- 4 **Conclusion**
- 5 **Bibliography**

## Why we need to scale

---

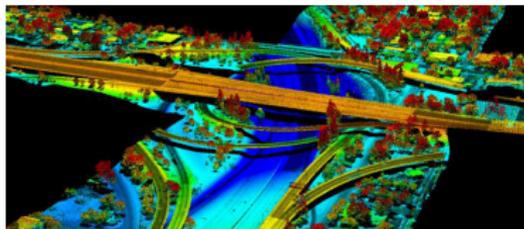
- **Problem:** best approaches are very memory-hungry and the data volumes are huge.



## Why we need to scale

---

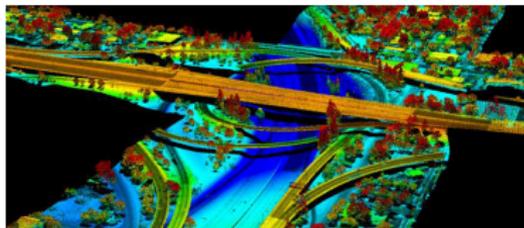
- **Problem:** best approaches are very memory-hungry and the data volumes are huge.
- Previous methods only works with a few thousands points.



## Why we need to scale

---

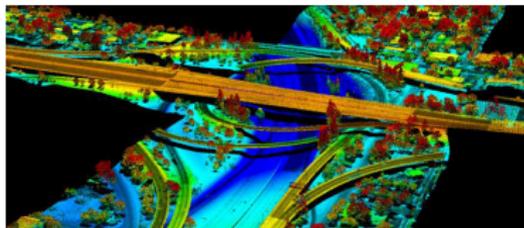
- **Problem:** best approaches are very memory-hungry and the data volumes are huge.
- Previous methods only works with a few thousands points.
- **Naive strategies:**
  - **Aggressive subsampling:** loses a lot of information.



## Why we need to scale

---

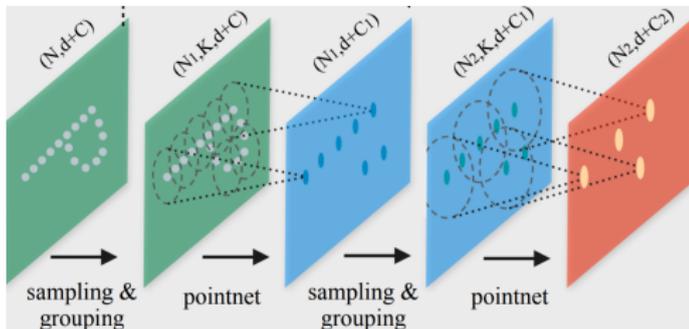
- **Problem:** best approaches are very memory-hungry and the data volumes are huge.
- Previous methods only works with a few thousands points.
- **Naive strategies:**
  - **Aggressive subsampling:** loses a lot of information.
  - **Sliding windows:** loses the global structure.



credit: tuck mapping solution

# PointNet++

- Pyramid structure for multi-scale feature extraction.

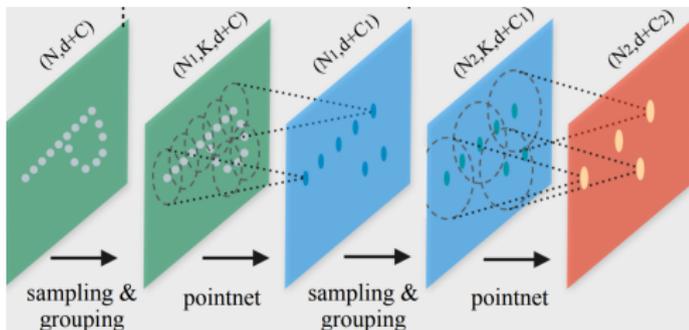


Qi et. al.2017b

credit: Qi et. al.2017b

# PointNet++

- Pyramid structure for multi-scale feature extraction.
- From local to global with with increasingly abstract features.

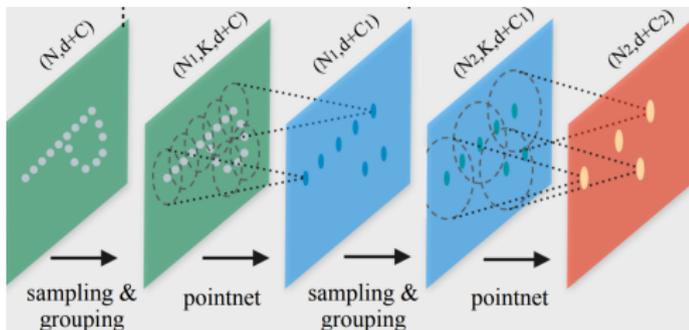


Qi et. al.2017b

credit: Qi et. al.2017b

# PointNet++

- Pyramid structure for multi-scale feature extraction.
- From local to global with with increasingly abstract features.
- Still require to process millions of points.



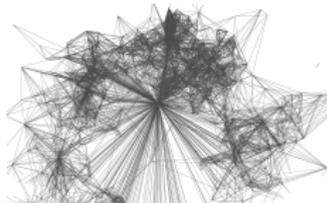
Qi et. al.2017b

credit: Qi et. al.2017b

# SuperPoint-Graph

- **Observation:**

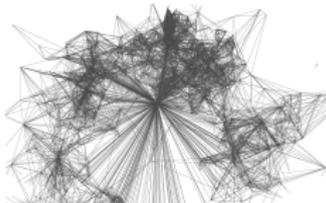
$n_{\text{points}} \gg n_{\text{objects}}$ .



Landrieu&Simonovski2018

# SuperPoint-Graph

- **Observation:**  
 $n_{\text{points}} \gg n_{\text{objects}}$ .
- Partition scene into superpoints with simple shapes.



Landrieu&Simonovski2018

# SuperPoint-Graph

- **Observation:**

$n_{\text{points}} \gg n_{\text{objects}}$ .

- Partition scene into superpoints with simple shapes.
- Only a few superpoints, context leveraging with powerful graph methods.



Landrieu&Simonovski2018

# Pipeline

---

- Semantic segmentation down to 3 sub-problems:

# Pipeline

---

- Semantic segmentation down to 3 sub-problems:
  - **Geometric Partition** : into simple shapes.  
Complexity: very high (clouds of  $10^8$  points)  
Algorithm:  $\ell_0$ -cut pursuit

# Pipeline

---

- Semantic segmentation down to 3 sub-problems:
  - **Geometric Partition** : into simple shapes.  
Complexity: very high (clouds of  $10^8$  points)  
Algorithm:  $\ell_0$ -cut pursuit
  - **Superpoint embedding**: learning shape descriptors  
Complexity: low (subsampling to 128 points  $\times$   $\sim$  1000 points)  
Algorithm: PointNet

# Pipeline

---

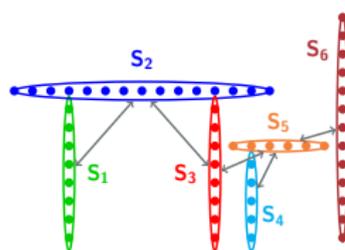
- Semantic segmentation down to 3 sub-problems:
  - **Geometric Partition** : into simple shapes.  
Complexity: very high (clouds of  $10^8$  points)  
Algorithm:  $\ell_0$ -cut pursuit
  - **Superpoint embedding**: learning shape descriptors  
Complexity: low (subsampling to 128 points  $\times$   $\sim$  1000 points)  
Algorithm: PointNet
  - **Contextual Segmentation**: using the global structure  
Complexity: very low (superpoint graph  $\sim$  1000 sp)  
Algorithm: ECC with Gated Recurrent Unit (GRU)

# Pipeline



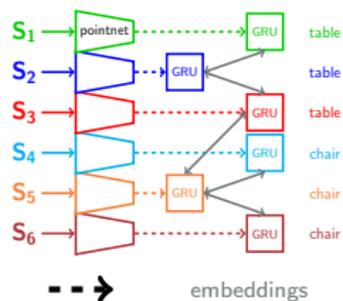
● point  
— Voronoi Edge

(a) Point cloud



○ superpoint  
↔ superedge

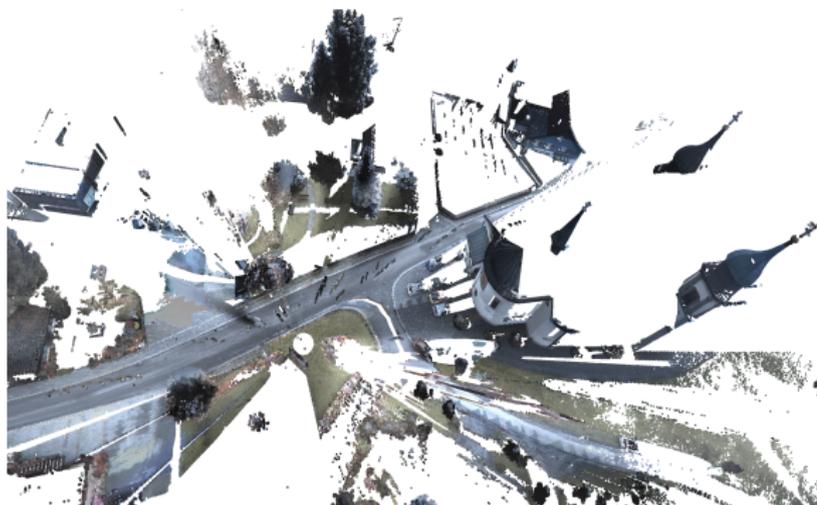
(b) Superpoint graph



(c) Convolution Network

## Qualitative Results: Semantic3D

Semantic3D: 3 billions points over 30 clouds



- route
- herbe
- arbre
- buisson
- bâtiment
- aménagement
- artefact
- voiture

## Qualitative Results: Semantic3D

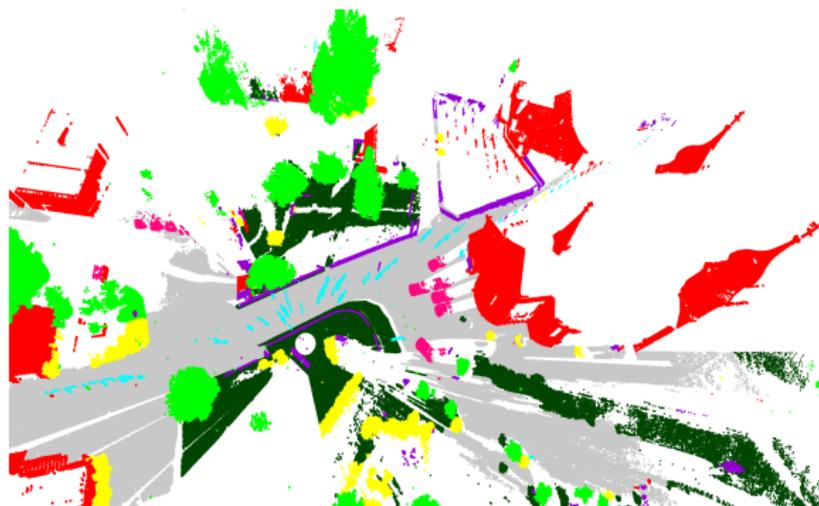
Semantic3D: 3 billions points over 30 clouds



- route
- herbe
- arbre
- buisson
- bâtiment
- aménagement
- artefact
- voiture

## Qualitative Results: Semantic3D

Semantic3D: 3 billions points over 30 clouds



- route
- herbe
- arbre
- buisson
- bâtiment
- aménagement
- artefact
- voiture

## Qualitative Results: Semantic3D

---

Semantic3D: 3 billions points over 30 clouds

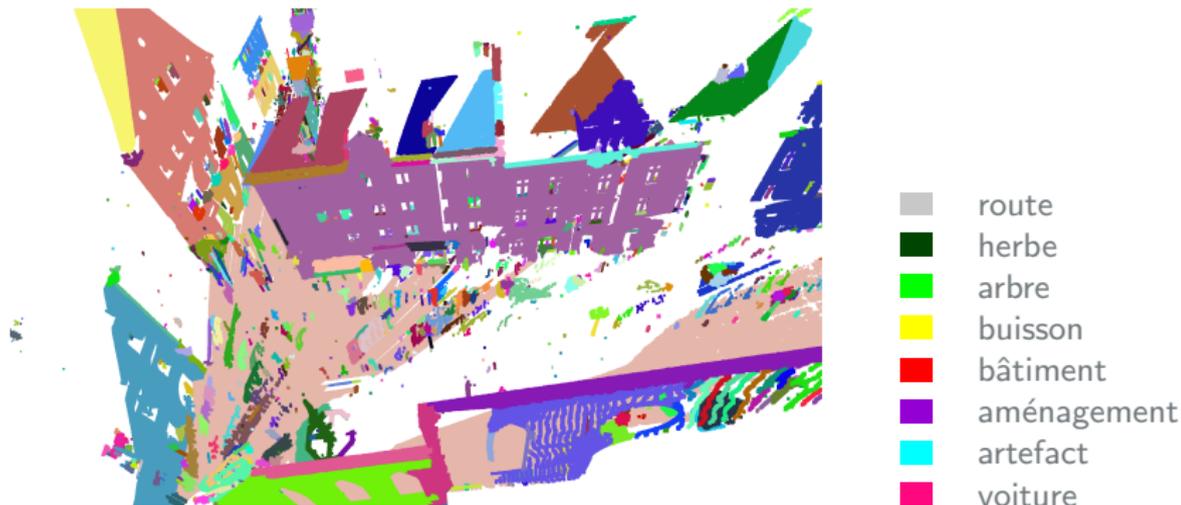


- route
- herbe
- arbre
- buisson
- bâtiment
- aménagement
- artefact
- voiture

## Qualitative Results: Semantic3D

---

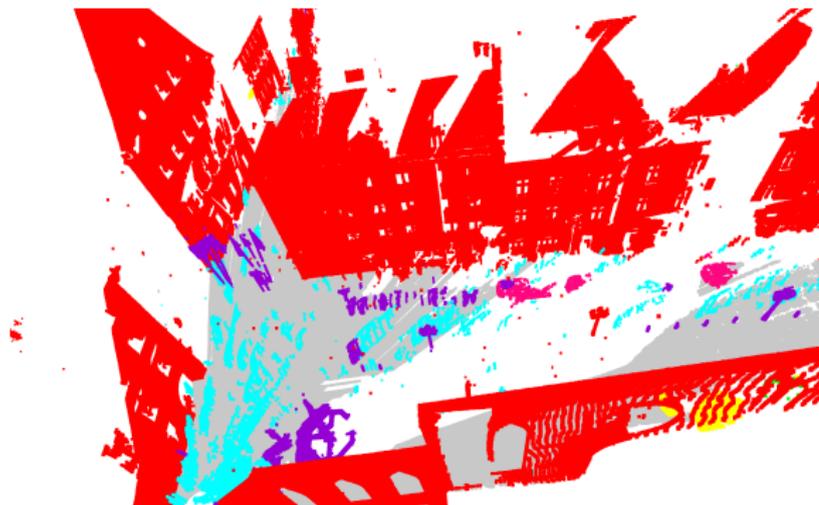
Semantic3D: 3 billions points over 30 clouds



## Qualitative Results: Semantic3D

---

Semantic3D: 3 billions points over 30 clouds



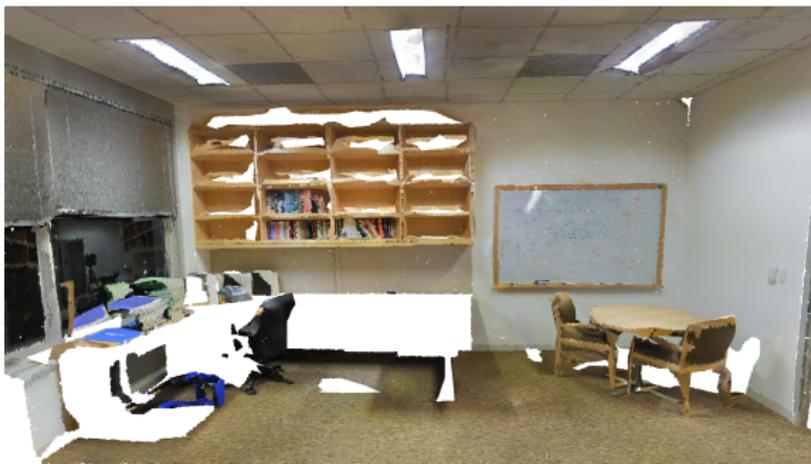
- route
- herbe
- arbre
- buisson
- bâtiment
- aménagement
- artefact
- voiture

## Quantitative Results: Semantic3D

Method	OA	mIoU	road	grass	tree	bush	building	hard-scape	artifact	cars
reduced test set: 78 699 329 points										
TMLC-MSR	86.2	54.2	89.8	74.5	53.7	26.8	88.8	18.9	36.4	44.7
DeePr3SS	88.9	58.5	85.6	83.2	74.2	32.4	89.7	18.5	25.1	59.2
SnapNet	88.6	59.1	82.0	77.3	79.7	22.9	91.1	18.4	37.3	64.4
SegCloud	88.1	61.3	83.9	66.0	86.0	40.5	91.1	30.9	27.5	64.3
SPG (Ours)	<b>94.0</b>	<b>73.2</b>	<b>97.4</b>	<b>92.6</b>	<b>87.9</b>	<b>44.0</b>	<b>93.2</b>	<b>31.0</b>	<b>63.5</b>	<b>76.2</b>
full test set: 2 091 952 018 points										
TMLC-MS	85.0	49.4	91.1	69.5	32.8	21.6	87.6	25.9	11.3	55.3
SnapNet	91.0	67.4	89.6	<b>79.5</b>	74.8	56.1	90.9	36.5	34.3	77.2
SPG (Ours)	<b>92.9</b>	<b>76.2</b>	<b>91.5</b>	75.6	<b>78.3</b>	<b>71.7</b>	<b>94.4</b>	<b>56.8</b>	<b>52.9</b>	<b>88.4</b>

## Qualitative Results: S3DIS

Indoor, 3 buildings, 6 stories, 200+ rooms, 600 000 000+ points



- ceiling
- ground
- wall
- column
- beam
- window
- door
- table
- chair
- bookcase
- board
- other

## Qualitative Results: S3DIS

Indoor, 3 buildings, 6 stories, 200+ rooms, 600 000 000+ points



- ceiling
- ground
- wall
- column
- beam
- window
- door
- table
- chair
- bookcase
- board
- other

## Qualitative Results: S3DIS

Indoor, 3 buildings, 6 stories, 200+ rooms, 600 000 000+ points



- ceiling
- ground
- wall
- column
- beam
- window
- door
- table
- chair
- bookcase
- board
- other

## Qualitative Results: S3DIS

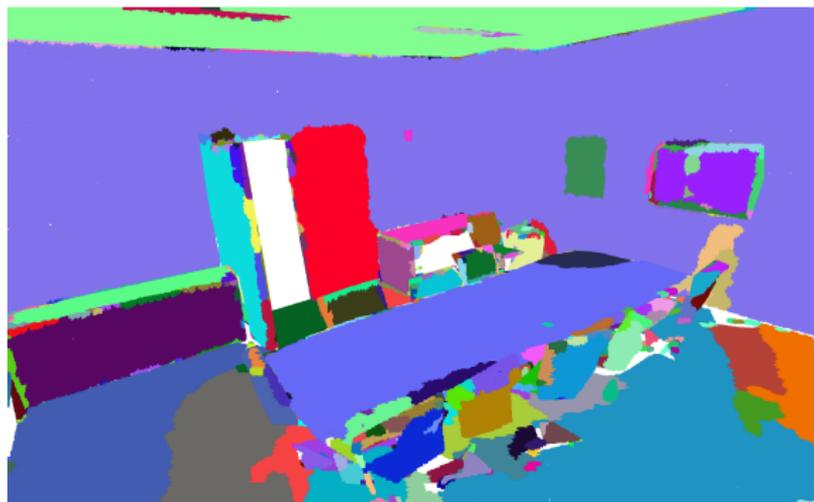
Indoor, 3 buildings, 6 stories, 200+ rooms, 600 000 000+ points



- ceiling
- ground
- wall
- column
- beam
- window
- door
- table
- chair
- bookcase
- board
- other

## Qualitative Results: S3DIS

Indoor, 3 buildings, 6 stories, 200+ rooms, 600 000 000+ points



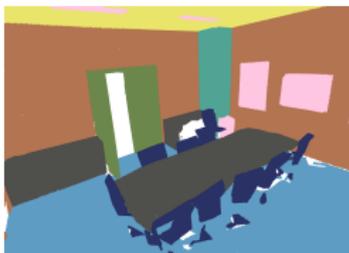
- ceiling
- ground
- wall
- column
- beam
- window
- door
- table
- chair
- bookcase
- board
- other

## Qualitative Results: S3DIS

Indoor, 3 buildings, 6 stories, 200+ rooms, 600 000 000+ points



## Résultats qualitatif: S3DIS



- ceiling
- ground
- wall
- column
- beam
- window
- door
- table
- chair
- bookcase
- board
- other

## Quantitative Results: S3DIS

---

Method	OA	mAcc	mIoU	door	board
A5 PointNet	–	48.5	41.1	10.7	<b>26.3</b>
A5 SEGCloud	–	57.3	48.9	23.1	13.0
<b>A5 SPG</b>	86.4	<b>66.5</b>	<b>58.0</b>	<b>61.5</b>	2.1
PointNet	78.5	66.2	47.6	51.6	29.4
Engelmann	81.1	66.4	49.7	51.2	<b>30.0</b>
<b>SPG</b>	<b>85.5</b>	<b>73.0</b>	<b>62.1</b>	<b>68.4</b>	8.7

## Quantitative Results: S3DIS

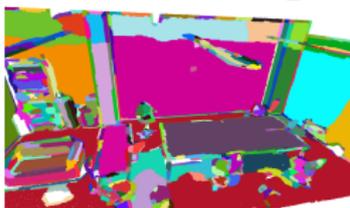
Method	OA	mAcc	mIoU	door	board
A5 PointNet	–	48.5	41.1	10.7	<b>26.3</b>
A5 SEGCloud	–	57.3	48.9	23.1	13.0
<b>A5 SPG</b>	86.4	<b>66.5</b>	<b>58.0</b>	<b>61.5</b>	2.1
PointNet	78.5	66.2	47.6	51.6	29.4
Engelmann	81.1	66.4	49.7	51.2	<b>30.0</b>
<b>SPG</b>	<b>85.5</b>	<b>73.0</b>	<b>62.1</b>	<b>68.4</b>	8.7

Step	Full cloud	2 cm	3 cm	4 cm
Voxelisation	0	40	24	16
Features	439	194	88	43
Partition	3428	1013	447	238
SPG computation	3800	958	436	252
Inference $\times 10$	240	110	60	50
Total	7907	2315	1055	599
mIoU 6-fold	54.1	60.2	62.1	57.1

# Superpoint Partition

$$f^* = \arg \min_{f \in \mathbb{R}^{C \times m}} \sum_{i \in C} \|f_i - e_i\|^2 + \sum_{(i,j) \in E} w_{i,j} [f_i \neq f_j],$$

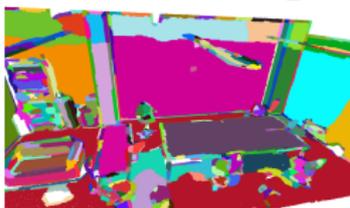
- $e \in \mathbb{R}^{C \times m}$  : handcrafted descriptors of the local geometry/radiometry



## Superpoint Partition

$$f^* = \arg \min_{f \in \mathbb{R}^{C \times m}} \sum_{i \in \mathcal{C}} \|f_i - e_i\|^2 + \sum_{(i,j) \in E} w_{i,j} [f_i \neq f_j],$$

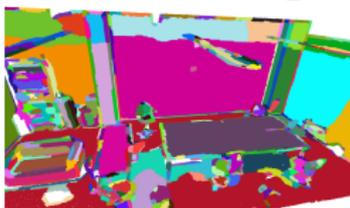
- $e \in \mathbb{R}^{C \times m}$  : handcrafted descriptors of the local geometry/radiometry
- Superpoints: connected components of a piecewise constant approximation of  $e$  structured by an adjacency graph.



## Superpoint Partition

$$f^* = \arg \min_{f \in \mathbb{R}^{C \times m}} \sum_{i \in \mathcal{C}} \|f_i - e_i\|^2 + \sum_{(i,j) \in E} w_{i,j} [f_i \neq f_j],$$

- $e \in \mathbb{R}^{C \times m}$  : handcrafted descriptors of the local geometry/radiometry
- Superpoints: connected components of a piecewise constant approximation of  $e$  structured by an adjacency graph.
- **Problem:** any errors made in the partition will carry in the prediction...



# Presentation Layout

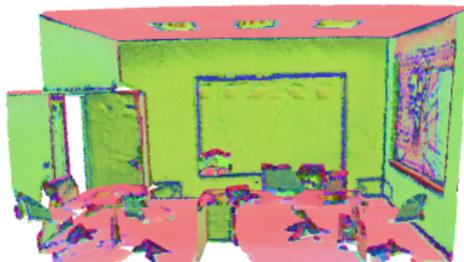
---

- 1 Deep Learning for 3D Point Clouds
- 2 Learning 3D Point Clouds Segmentation**
- 3 The Cut Pursuit Algorithm
- 4 Conclusion
- 5 Bibliography

# The Pipeline



Input Point Cloud



Learned Embedding



Oversegmentation



True Objects

## General idea:

- 1) Train a neural network to produce points embeddings with high contrast at the border of objects...
- 2) ... Which serve as inputs of a **nondifferentiable** segmentation algorithm.

# Adjacency Graph

---

- $G = (C, E)$  a meaningful adjacency graph



# Adjacency Graph

---

- $G = (C, E)$  a meaningful adjacency graph
- Construction is problem-dependant



# Adjacency Graph

---

- $G = (C, E)$  a meaningful adjacency graph
- Construction is problem-dependant
- $E_{\text{inter}}$  : set of inter-object edges



# Adjacency Graph

---

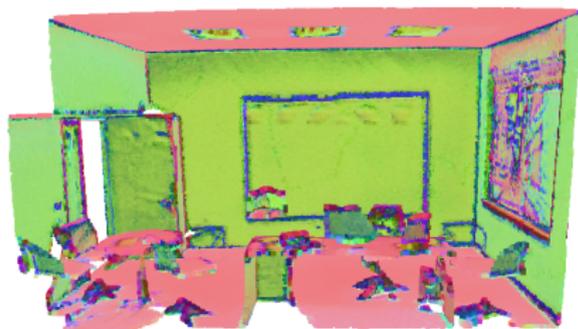
- $G = (C, E)$  a meaningful adjacency graph
- Construction is problem-dependant
- $E_{\text{inter}}$  : set of inter-object edges
- $E_{\text{intra}}$  : set of intra-object edges



# Adjacency Graph

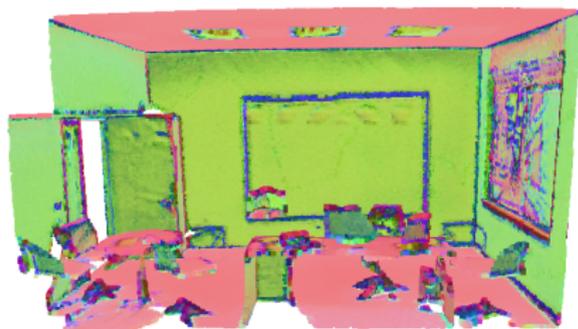
---

- $G = (C, E)$  a meaningful adjacency graph
- Construction is problem-dependant
- $E_{inter}$  : set of inter-object edges
- $E_{intra}$  : set of intra-object edges
- We want embeddings with high contrast at  $E_{inter}$  and similar value at  $E_{intra}$



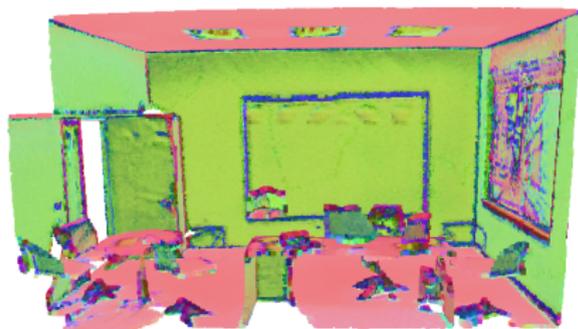
# Adjacency Graph

- $G = (C, E)$  a meaningful adjacency graph
- Construction is problem-dependant
- $E_{\text{inter}}$  : set of inter-object edges
- $E_{\text{intra}}$  : set of intra-object edges
- We want embeddings with high contrast at  $E_{\text{inter}}$  and similar value at  $E_{\text{intra}}$
- If we get  $E_{\text{inter}}$  right, then we have automatically object purity!



# Adjacency Graph

- $G = (C, E)$  a meaningful adjacency graph
- Construction is problem-dependant
- $E_{\text{inter}}$  : set of inter-object edges
- $E_{\text{intra}}$  : set of intra-object edges
- We want embeddings with high contrast at  $E_{\text{inter}}$  and similar value at  $E_{\text{intra}}$
- If we get  $E_{\text{inter}}$  right, then we have automatically object purity!  
**almost!**



## Generalized Minimal Partition Problem

---

- $e_i$  embeddings of the local geometry/radiometry

## Generalized Minimal Partition Problem

---

- $e_i$  embeddings of the local geometry/radiometry
- **Idea:** Superpoints are the component of a **piecewise-constant approximation** of the embeddings

$$f^* = \arg \min_{f \in \mathbb{R}^{C \times m}} \sum_{i \in C} \|f_i - e_i\|^2 + \sum_{(i,j) \in E} w_{i,j} [f_i \neq f_j],$$

## Generalized Minimal Partition Problem

---

- $e_i$  embeddings of the local geometry/radiometry
- **Idea:** Superpoints are the component of a **piecewise-constant approximation** of the embeddings

$$f^* = \arg \min_{f \in \mathbb{R}^{C \times m}} \sum_{i \in C} \|f_i - e_i\|^2 + \sum_{(i,j) \in E} w_{i,j} [f_i \neq f_j],$$

- Superpoints: regions with homogeneous embeddings

## Generalized Minimal Partition Problem

---

- $e_i$  embeddings of the local geometry/radiometry
- **Idea:** Superpoints are the component of a **piecewise-constant approximation** of the embeddings

$$f^* = \arg \min_{f \in \mathbb{R}^{C \times m}} \sum_{i \in C} \|f_i - e_i\|^2 + \sum_{(i,j) \in E} w_{i,j} [f_i \neq f_j],$$

- Superpoints: regions with homogeneous embeddings
- Works well with handcrafted embeddings, should work with learned ones!

## Generalized Minimal Partition Problem

---

- $e_i$  embeddings of the local geometry/radiometry
- **Idea:** Superpoints are the component of a **piecewise-constant approximation** of the embeddings

$$f^* = \arg \min_{f \in \mathbb{R}^{C \times m}} \sum_{i \in C} \|f_i - e_i\|^2 + \sum_{(i,j) \in E} w_{i,j} [f_i \neq f_j],$$

- Superpoints: regions with homogeneous embeddings
- Works well with handcrafted embeddings, should work with learned ones!
- **Problem:** a non-convex, nondifferentiable, noncontinuous problem

## Generalized Minimal Partition Problem

---

- $e_i$  embeddings of the local geometry/radiometry
- **Idea:** Superpoints are the component of a **piecewise-constant approximation** of the embeddings

$$f^* = \arg \min_{f \in \mathbb{R}^{C \times m}} \sum_{i \in C} \|f_i - e_i\|^2 + \sum_{(i,j) \in E} w_{i,j} [f_i \neq f_j],$$

- Superpoints: regions with homogeneous embeddings
- Works well with handcrafted embeddings, should work with learned ones!
- **Problem:** a non-convex, nondifferentiable, noncontinuous problem
- Good approximations can be computed with  $\ell_0$ -cut pursuit [Landrieu & Obozinski SIIMS 2018]

## The Problem With the GMPP

---

$$f^* = \arg \min_{f \in \mathbb{R}^{C \times m}} \sum_{i \in C} \|f_i - e_i\|^2 + \sum_{(i,j) \in E} w_{i,j} [f_i \neq f_j],$$

- Let consider our pipeline:

## The Problem With the GMPP

---

$$f^* = \arg \min_{f \in \mathbb{R}^{C \times m}} \sum_{i \in C} \|f_i - e_i\|^2 + \sum_{(i,j) \in E} w_{i,j} [f_i \neq f_j],$$

- Let consider our pipeline:
  - Let  $x$  be the parameters of the Local Point Embedder

## The Problem With the GMPP

---

$$f^* = \arg \min_{f \in \mathbb{R}^{C \times m}} \sum_{i \in C} \|f_i - e_i\|^2 + \sum_{(i,j) \in E} w_{i,j} [f_i \neq f_j],$$

- Let consider our pipeline:
  - Let  $x$  be the parameters of the Local Point Embedder
  - Let  $e(x)$  be the resulting embeddings

## The Problem With the GMPP

---

$$f^* = \arg \min_{f \in \mathbb{R}^{C \times m}} \sum_{i \in C} \|f_i - e_i\|^2 + \sum_{(i,j) \in E} w_{i,j} [f_i \neq f_j],$$

- Let consider our pipeline:
  - Let  $x$  be the parameters of the Local Point Embedder
  - Let  $e(x)$  be the resulting embeddings
  - Let  $f^*(e(x))$  be the solution of the GMPP

## The Problem With the GMPP

---

$$f^* = \arg \min_{f \in \mathbb{R}^{C \times m}} \sum_{i \in C} \|f_i - e_i\|^2 + \sum_{(i,j) \in E} w_{i,j} [f_i \neq f_j],$$

- Let consider our pipeline:
  - Let  $x$  be the parameters of the Local Point Embedder
  - Let  $e(x)$  be the resulting embeddings
  - Let  $f^*(e(x))$  be the solution of the GMPP
  - Let  $CCC$  the constant connected component operator on  $G$
  - The superpoints are:  $S = CCC(f^*(e(x)))$

## The Problem With the GMPP

---

$$f^* = \arg \min_{f \in \mathbb{R}^{C \times m}} \sum_{i \in C} \|f_i - e_i\|^2 + \sum_{(i,j) \in E} w_{i,j} [f_i \neq f_j],$$

- Let consider our pipeline:
  - Let  $x$  be the parameters of the Local Point Embedder
  - Let  $e(x)$  be the resulting embeddings
  - Let  $f^*(e(x))$  be the solution of the GMPP
  - Let  $CCC$  the constant connected component operator on  $G$
  - The superpoints are:  $S = CCC(f^*(e(x)))$
- Let  $M(S)$  be a measure of how good an oversegmentation is (implementing purity, border recall, etc...)

## The Problem With the GMPP

---

$$f^* = \arg \min_{f \in \mathbb{R}^{C \times m}} \sum_{i \in C} \|f_i - e_i\|^2 + \sum_{(i,j) \in E} w_{i,j} [f_i \neq f_j],$$

- Let consider our pipeline:
  - Let  $x$  be the parameters of the Local Point Embedder
  - Let  $e(x)$  be the resulting embeddings
  - Let  $f^*(e(x))$  be the solution of the GMPP
  - Let  $CCC$  the constant connected component operator on  $G$
  - The superpoints are:  $S = CCC(f^*(e(x)))$
- Let  $M(S)$  be a measure of how good an oversegmentation is (implementing purity, border recall, etc...)
- **Naive Approach:**  $\ell(x) = -M(CCC(f^*(e(x))))$

## The Problem With the GMPP

---

$$f^* = \arg \min_{f \in \mathbb{R}^{C \times m}} \sum_{i \in C} \|f_i - e_i\|^2 + \sum_{(i,j) \in E} w_{i,j} [f_i \neq f_j],$$

- Let consider our pipeline:
  - Let  $x$  be the parameters of the Local Point Embedder
  - Let  $e(x)$  be the resulting embeddings
  - Let  $f^*(e(x))$  be the solution of the GMPP
  - Let  $CCC$  the constant connected component operator on  $G$
  - The superpoints are:  $S = CCC(f^*(e(x)))$
- Let  $M(S)$  be a measure of how good an oversegmentation is (implementing purity, border recall, etc...)
- **Naive Approach:**  $\ell(x) = -M(CCC(f^*(e(x))))$
- To backpropagate we need:  $\frac{\partial CCC}{\partial f^*}$  and  $\frac{\partial f^*}{\partial e}$

## The Problem With the GMPP

---

$$f^* = \arg \min_{f \in \mathbb{R}^{C \times m}} \sum_{i \in C} \|f_i - e_i\|^2 + \sum_{(i,j) \in E} w_{i,j} [f_i \neq f_j],$$

- Let consider our pipeline:
  - Let  $x$  be the parameters of the Local Point Embedder
  - Let  $e(x)$  be the resulting embeddings
  - Let  $f^*(e(x))$  be the solution of the GMPP
  - Let  $CCC$  the constant connected component operator on  $G$
  - The superpoints are:  $S = CCC(f^*(e(x)))$
- Let  $M(S)$  be a measure of how good an oversegmentation is (implementing purity, border recall, etc...)
- **Naive Approach:**  $\ell(x) = -M(CCC(f^*(e(x))))$
- To backpropagate we need:  $\frac{\partial CCC}{\partial f^*}$  and  $\frac{\partial f^*}{\partial e}$
- **Problem:** Those functions are **not backpropagable**.

## Graph-Structured Contrastive Loss

---

- We propose a *surrogate* loss to learn meaningful embeddings

$$\ell(e) = \frac{1}{|E|} \left( \sum_{(i,j) \in E_{\text{intra}}} \phi(\mathbf{e}_i - \mathbf{e}_j) + \sum_{(i,j) \in E_{\text{inter}}} \mu_{i,j} \psi(\mathbf{e}_i - \mathbf{e}_j) \right),$$

## Graph-Structured Contrastive Loss

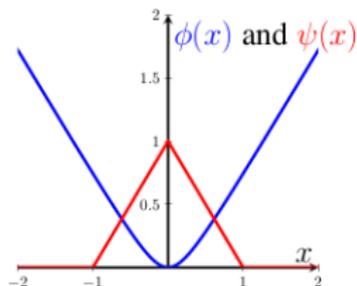
- We propose a *surrogate* loss to learn meaningful embeddings

$$\ell(e) = \frac{1}{|E|} \left( \sum_{(i,j) \in E_{\text{intra}}} \phi(e_i - e_j) + \sum_{(i,j) \in E_{\text{inter}}} \mu_{i,j} \psi(e_i - e_j) \right),$$

- $\phi$  minimum at 0,  $\psi$  maximum at 0

$$\phi(x) = \delta(\sqrt{\|x\|^2/\delta^2 + 1} - 1)$$

$$\psi(x) = \max(1 - \|x\|, 0)$$



## Graph-Structured Contrastive Loss

- We propose a *surrogate* loss to learn meaningful embeddings

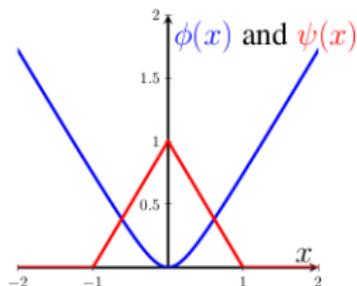
$$\ell(e) = \frac{1}{|E|} \left( \sum_{(i,j) \in E_{\text{intra}}} \phi(e_i - e_j) + \sum_{(i,j) \in E_{\text{inter}}} \mu_{i,j} \psi(e_i - e_j) \right),$$

- $\phi$  minimum at 0,  $\psi$  maximum at 0

$$\phi(x) = \delta(\sqrt{\|x\|^2/\delta^2 + 1} - 1)$$

$$\psi(x) = \max(1 - \|x\|, 0)$$

- Promotes homogeneity within objects and contrast at their borders



## Graph-Structured Contrastive Loss

- We propose a *surrogate* loss to learn meaningful embeddings

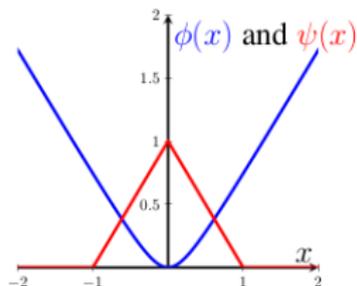
$$\ell(e) = \frac{1}{|E|} \left( \sum_{(i,j) \in E_{\text{intra}}} \phi(e_i - e_j) + \sum_{(i,j) \in E_{\text{inter}}} \mu_{i,j} \psi(e_i - e_j) \right),$$

- $\phi$  minimum at 0,  $\psi$  maximum at 0

$$\phi(x) = \delta(\sqrt{\|x\|^2/\delta^2 + 1} - 1)$$

$$\psi(x) = \max(1 - \|x\|, 0)$$

- Promotes homogeneity within objects and contrast at their borders
- $\mu_{i,j}$  : weight of inter-edges



## Cross-Partition Weighting Strategy, cont'd

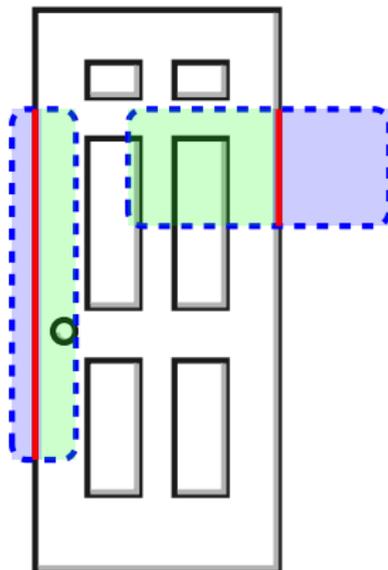
$$\mu_{U,V} = \mu \frac{\min(|U|, |V|)}{|(U, V)|} \quad \text{for } (U, V) \in \mathcal{E} \quad \mu_{i,j} = \mu_{U,V} \text{ for all } (i,j) \in (U, V)$$

- Role of  $\mu_{i,j}$  critical: assess impact of missed edge.
- Operate on  $\mathcal{G} = (\mathcal{V}, \mathcal{E})$  adjacency graph of cross-partition between superpoints and real objects.

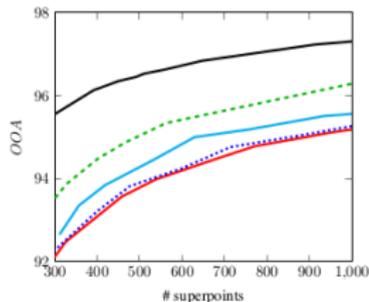


$$\mu_{LW,LD} = \frac{\text{[Diagram: blue dashed box on top, red line below]}}{\text{[Diagram: red line below]}}$$

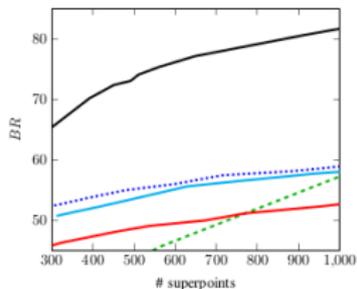
$$\mu_{RW,RD} = \frac{\text{[Diagram: blue dashed box on top, red line below]}}{\text{[Diagram: red line below]}}$$



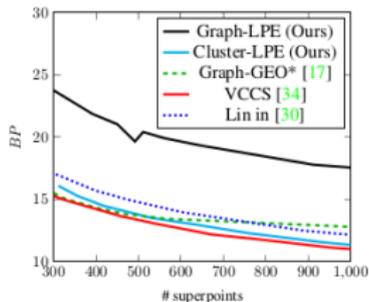
# Results



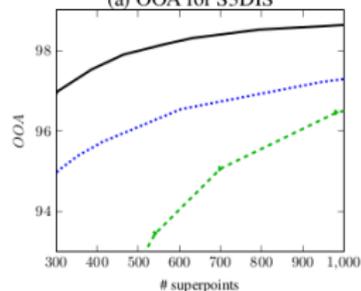
(a) OOA for S3DIS



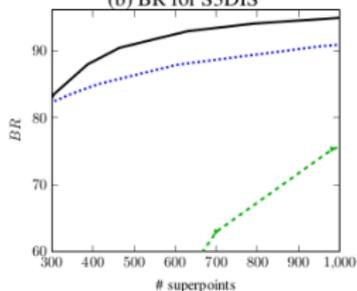
(b) BR for S3DIS



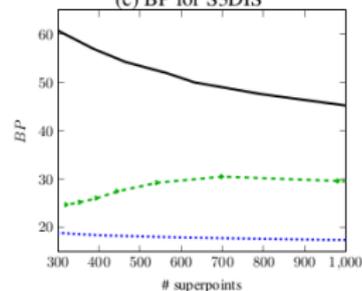
(c) BP for S3DIS



(d) OOA for vKITTI



(e) BR for vKITTI



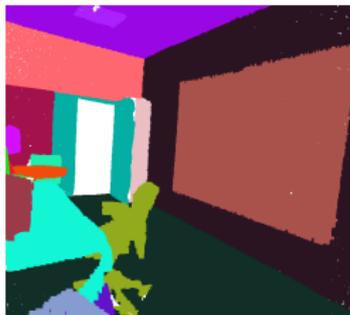
(f) BP for vKITTI

**We require 5 times less superpoints for similar performance!**

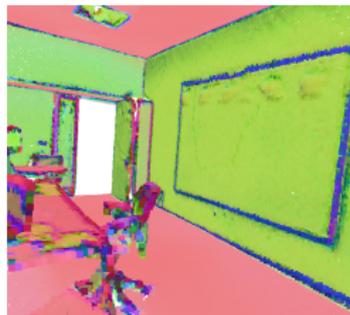
# Illustration



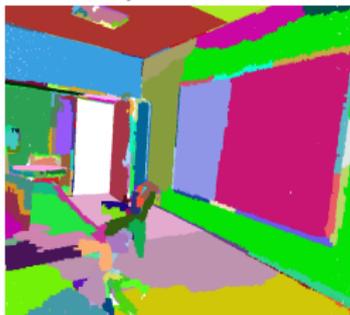
Input cloud



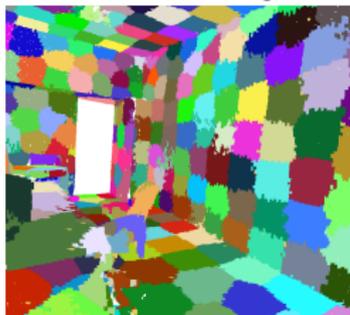
Ground truth objects



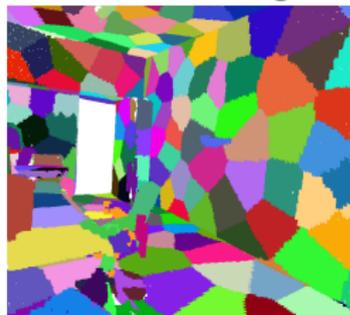
LPE embeddings



Graph-LPE (ours)



VCCS, Papon *et al.* 2013

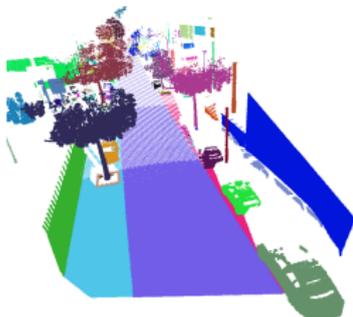


Lin *et al.* 2018

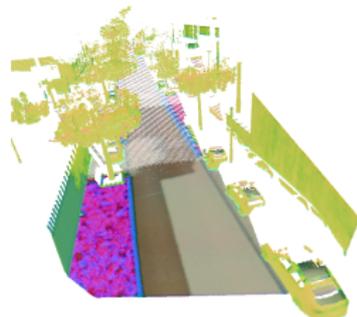
# Illustration



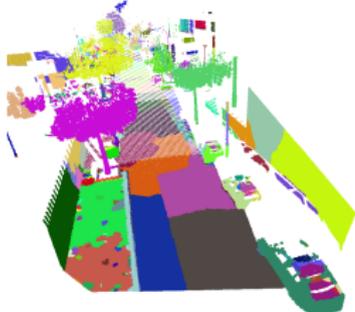
Input cloud



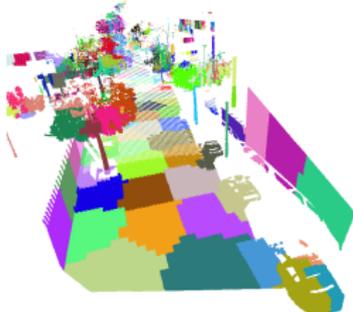
Ground truth objects



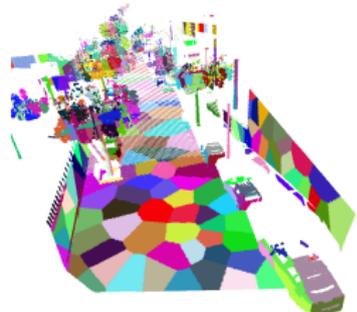
LPE embeddings



Graph-LPE (ours)



VCCS, Papon *et al.* 2013



Lin *et al.* 2018

# Results

Method	OA	mAcc	mIoU
6-fold cross validation			
PointNet 2017	78.5	66.2	47.6
Engelmann <i>et al.</i> in 2017	81.1	66.4	49.7
PointNet++ 2017	81.0	67.1	54.5
Engelmann <i>et al.</i> in 2018	84.0	67.8	58.3
SPG 2018	85.5	73.0	62.1
PointCNN 2018	<b>88.1</b>	75.6	65.4
Graph-LPE + SPG (ours)	87.8	<b>77.5</b>	<b>67.6</b>
Fold 5			
PointNet 2017	-	49.0	41.1
Engelmann <i>et al.</i> in 2018	84.2	61.8	52.2
pointCNN 2018	85.9	63.9	57.3
SPG 2018	86.4	66.5	58.0
PCCN 2018	-	67.0	58.3
Graph-LPE + SPG (ours)	<b>87.8</b>	<b>69.1</b>	<b>61.5</b>

Table: S3DIS

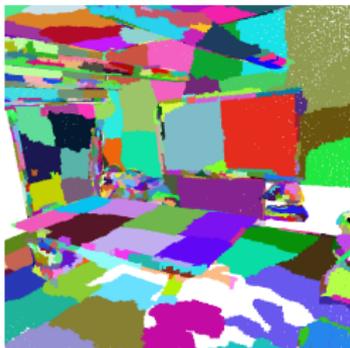
Method	OA	mAcc	mIoU
PointNet 2017	79.7	47.0	34.4
Engelmann 2018	79.7	57.6	35.6
Engelmann 2017	80.6	49.7	36.2
3P-RNN 2018	<b>87.8</b>	54.1	41.6
Graph-LPE + SPG (ours)	85.2	<b>62.4</b>	<b>49.7</b>

Table: vKITTI

# Illustration



Input Cloud



Oversegmentation

## S3DIS

- ceiling
- floor
- wall
- column
- beam
- window
- door
- table
- chair
- bookcase
- sofa
- board
- clutter
- unlabelled



prediction

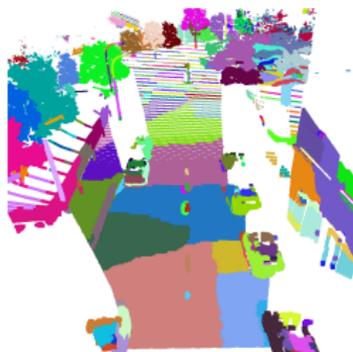


Ground Truth

# Illustration



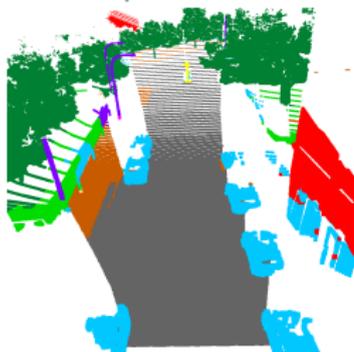
Input Cloud



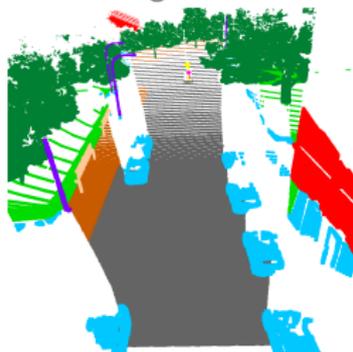
Oversegmentation

## vKITTI

- terrain
- tree
- vegetation
- building
- road
- guard rail
- traffic sign
- traffic light
- pole
- misc
- truck
- car
- van
- unlabelled



prediction



Ground Truth

# Presentation Layout

---

- 1 Deep Learning for 3D Point Clouds
- 2 Learning 3D Point Clouds Segmentation
- 3 The Cut Pursuit Algorithm**
- 4 Conclusion
- 5 Bibliography

## the Cut-Pursuit Algorithm

---

- A working-set approach to graph-structured spatial regularization

## the Cut-Pursuit Algorithm

---

- A working-set approach to graph-structured spatial regularization
- Joint work with Guillaume Obozinski and Hugo Raguet

L. Landrieu and G. Obozinski. Cut Pursuit: Fast Algorithms to Learn Piecewise Constant Functions. In AISTATS, 2016

L. Landrieu and G. Obozinski. Cut pursuit: Fast Algorithms to Learn Piecewise Constant Functions on General Weighted Graphs. SIAM Journal on Imaging Sciences, 2017

H. Raguet and L. Landrieu. Cut-pursuit Algorithm for Regularizing Nonsmooth Functionals With Graph Total Variation. In ICML, 2018

## the Cut-Pursuit Algorithm

---

- A working-set approach to graph-structured spatial regularization
- Joint work with Guillaume Obozinski and Hugo Raguet
- Initially designed for graph-total variation minimization

L. Landrieu and G. Obozinski. Cut Pursuit: Fast Algorithms to Learn Piecewise Constant Functions. In AISTATS, 2016

L. Landrieu and G. Obozinski. Cut pursuit: Fast Algorithms to Learn Piecewise Constant Functions on General Weighted Graphs. SIAM Journal on Imaging Sciences, 2017

H. Raguet and L. Landrieu. Cut-pursuit Algorithm for Regularizing Nonsmooth Functionals With Graph Total Variation. In ICML, 2018

## the Cut-Pursuit Algorithm

---

- A working-set approach to graph-structured spatial regularization
- Joint work with Guillaume Obozinski and Hugo Raguet
- Initially designed for graph-total variation minimization
- Can be generalized to the nonconvex setting of the GMMP.

L. Landrieu and G. Obozinski. Cut Pursuit: Fast Algorithms to Learn Piecewise Constant Functions. In AISTATS, 2016

L. Landrieu and G. Obozinski. Cut pursuit: Fast Algorithms to Learn Piecewise Constant Functions on General Weighted Graphs. SIAM Journal on Imaging Sciences, 2017

H. Raguet and L. Landrieu. Cut-pursuit Algorithm for Regularizing Nonsmooth Functionals With Graph Total Variation. In ICML, 2018

## the Cut-Pursuit Algorithm

---

- A working-set approach to graph-structured spatial regularization
- Joint work with Guillaume Obozinski and Hugo Raguet
- Initially designed for graph-total variation minimization
- Can be generalized to the nonconvex setting of the GMMP.
- **Main Idea:** exploiting the coarseness of the solutions of such problem.

L. Landrieu and G. Obozinski. Cut Pursuit: Fast Algorithms to Learn Piecewise Constant Functions. In AISTATS, 2016

L. Landrieu and G. Obozinski. Cut pursuit: Fast Algorithms to Learn Piecewise Constant Functions on General Weighted Graphs. SIAM Journal on Imaging Sciences, 2017

H. Raguet and L. Landrieu. Cut-pursuit Algorithm for Regularizing Nonsmooth Functionals With Graph Total Variation. In ICML, 2018

## Objective

$$x^* = \arg \min_{x \in \mathbb{R}^V} f(x) + \sum_{v \in V} g_v(x) + \sum_{(u,v) \in E} w_{(u,v)} |x_u - x_v|$$

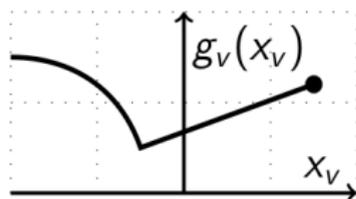
differentiable

dir. derivative in  $] -\infty, \infty]$

ex:  $|\cdot|, \iota_{\Omega}(\cdot)$

graph total variation

- Optimization problem structured by  $G = (V, E, w)$



# Objective

$$x^* = \arg \min_{x \in \mathbb{R}^V} f(x) + \sum_{v \in V} g_v(x) + \sum_{(u,v) \in E} w_{(u,v)} |x_u - x_v|$$

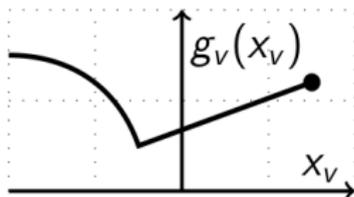
differentiable

dir. derivative in  $] - \infty, \infty ]$

ex:  $|\cdot|, \iota_{\Omega}(\cdot)$

graph total variation

- Optimization problem structured by  $G = (V, E, w)$
- Fairly general formulation



# Objective

$$x^* = \arg \min_{x \in \mathbb{R}^V} f(x) + \sum_{v \in V} g_v(x) + \sum_{(u,v) \in E} w_{(u,v)} |x_u - x_v|$$

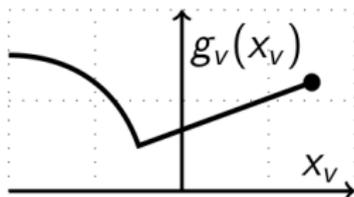
differentiable

dir. derivative in  $] - \infty, \infty]$

ex:  $|\cdot|, \iota_{\Omega}(\cdot)$

graph total variation

- Optimization problem structured by  $G = (V, E, w)$
- Fairly general formulation
- Includes inverse problems:  $f(x) = \|Ax - y\|^2$



## Objective

$$x^* = \arg \min_{x \in \mathbb{R}^V} f(x) + \sum_{v \in V} g_v(x) + \sum_{(u,v) \in E} w_{(u,v)} |x_u - x_v|$$

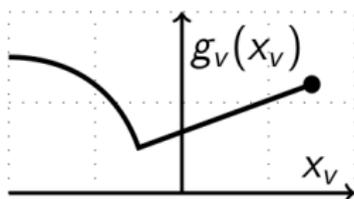
differentiable

dir. derivative in  $] -\infty, \infty]$

ex:  $|\cdot|, \iota_{\Omega}(\cdot)$

graph total variation

- Optimization problem structured by  $G = (V, E, w)$
- Fairly general formulation
- Includes inverse problems:  $f(x) = \|Ax - y\|^2$
- L1 fidelity:  $f(x) = 0, g_v(x) = |x_v - y_v|$



## Objective

$$x^* = \arg \min_{x \in \mathbb{R}^V} f(x) + \sum_{v \in V} g_v(x) + \sum_{(u,v) \in E} w_{(u,v)} |x_u - x_v|$$

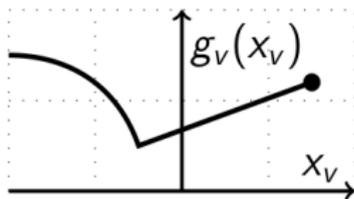
differentiable

dir. derivative in  $] -\infty, \infty]$

ex:  $|\cdot|, \iota_{\Omega}(\cdot)$

graph total variation

- Optimization problem structured by  $G = (V, E, w)$
- Fairly general formulation
- Includes inverse problems:  $f(x) = \|Ax - y\|^2$
- L1 fidelity:  $f(x) = 0, g_v(x) = |x_v - y_v|$
- Fused lasso regularization:  $g_v(x) = |x_v|$



## Objective

$$x^* = \arg \min_{x \in \mathbb{R}^V} f(x) + \sum_{v \in V} g_v(x) + \sum_{(u,v) \in E} w_{(u,v)} |x_u - x_v|$$

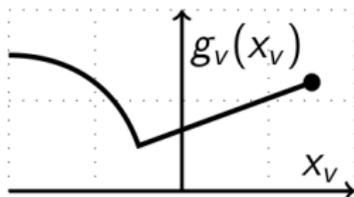
differentiable

dir. derivative in  $] -\infty, \infty]$

ex:  $|\cdot|, \iota_{\Omega}(\cdot)$

graph total variation

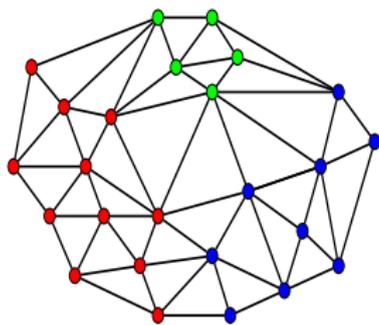
- Optimization problem structured by  $G = (V, E, w)$
- Fairly general formulation
- Includes inverse problems:  $f(x) = \|Ax - y\|^2$
- L1 fidelity:  $f(x) = 0, g_v(x) = |x_v - y_v|$
- Fused lasso regularization:  $g_v(x) = |x_v|$
- No convexity requirement.



# Motivation

---

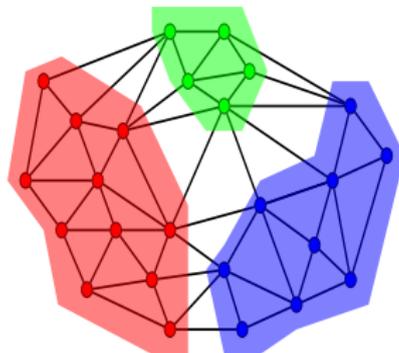
- TV regularization  $\Rightarrow$  solution piecewise constant.



# Motivation

---

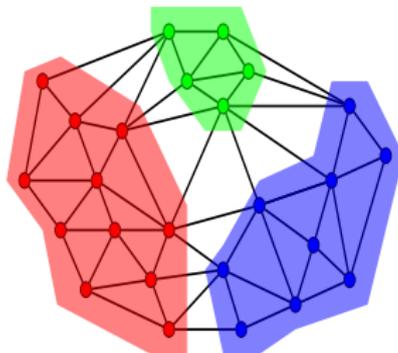
- TV regularization  $\Rightarrow$  solution piecewise constant.



# Motivation

---

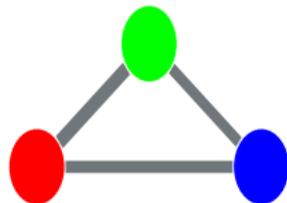
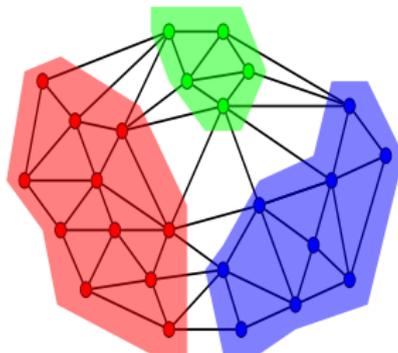
- TV regularization  $\Rightarrow$  solution piecewise constant.
- What if we knew this partition in advance?



# Motivation

---

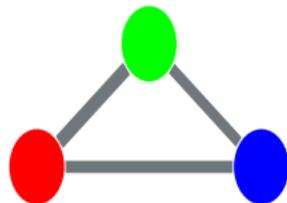
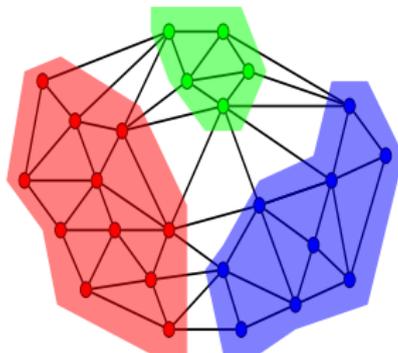
- TV regularization  $\Rightarrow$  solution piecewise constant.
- What if we knew this partition in advance?
- We could solve the problem on a much smaller **reduced graph**.



# Motivation

---

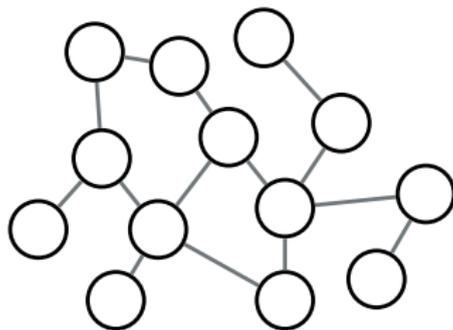
- TV regularization  $\Rightarrow$  solution piecewise constant.
- What if we knew this partition in advance?
- We could solve the problem on a much smaller **reduced graph**.
- TV regularization constrained to piecewise constant solutions wrt a partition of  $G \Leftrightarrow$  TV regularization wrt. the reduced graph.



## Principle

---

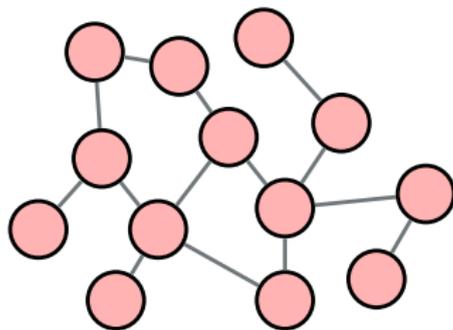
- 1 • Start with a trivial partition  
 $P = \{V\}$



# Principle

---

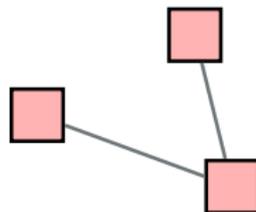
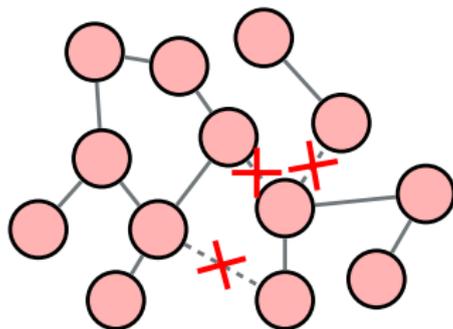
- 1 Start with a trivial partition  
 $P = \{V\}$
- 2 • Solve problem on reduced graph induced by  $P$



# Principle

---

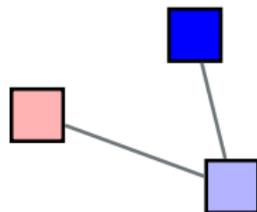
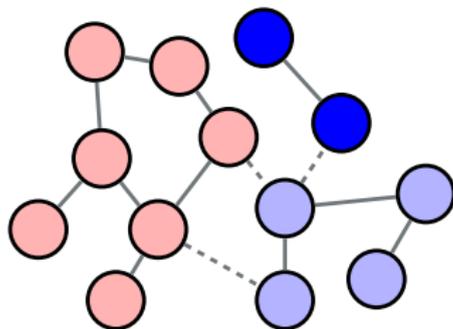
- 1 Start with a trivial partition  
 $P = \{V\}$
- 2 Solve problem on reduced graph induced by  $P$
- 3 • Refine current partition  $P$



# Principle

---

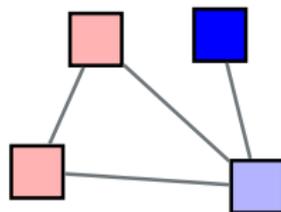
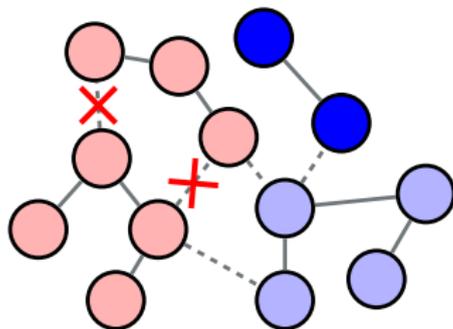
- 1 Start with a trivial partition  
 $P = \{V\}$
- 2 • Solve problem on reduced graph induced by  $P$
- 3 Refine current partition  $P$



# Principle

---

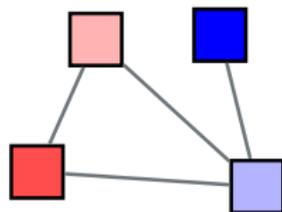
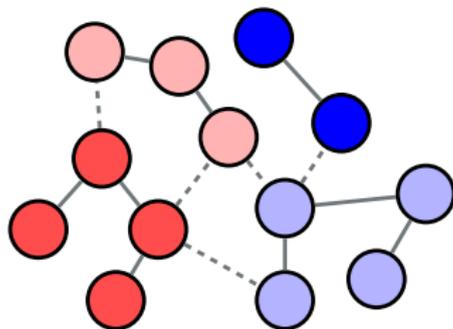
- 1 Start with a trivial partition  
 $P = \{V\}$
- 2 Solve problem on reduced graph induced by  $P$
- 3 • Refine current partition  $P$



# Principle

---

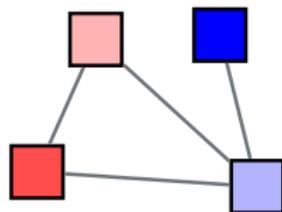
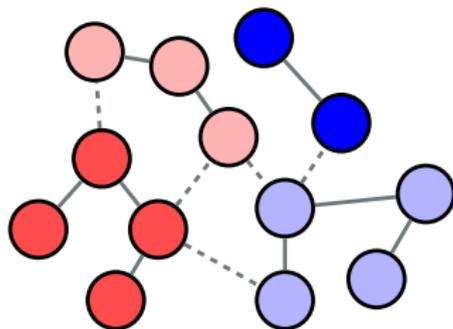
- 1 Start with a trivial partition  
 $P = \{V\}$
- 2 • Solve problem on reduced graph induced by  $P$
- 3 Refine current partition  $P$



# Principle

---

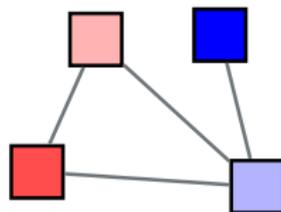
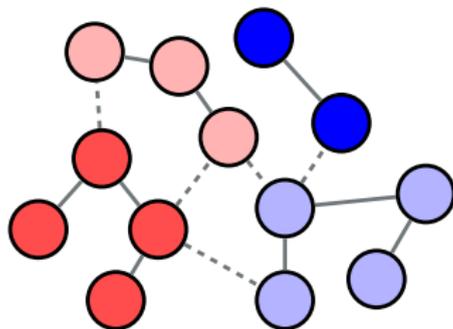
- 1 Start with a trivial partition  
 $P = \{V\}$
- 2 Solve problem on reduced graph induced by  $P$
- 3 • Refine current partition  $P$



# Principle

---

- 1 Start with a trivial partition  
 $P = \{V\}$
- 2 Solve problem on reduced graph induced by  $P$
- 3 Refine current partition  $P$
- 4 ● Critical point found.

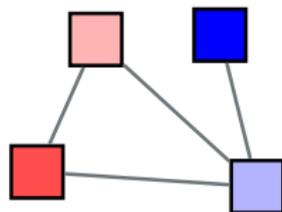
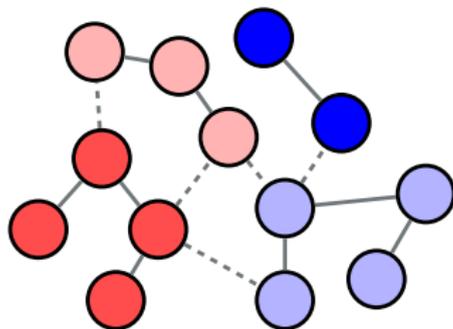


# Principle

---

- 1 Start with a trivial partition  
 $P = \{V\}$
- 2 Solve problem on reduced graph induced by  $P$
- 3 Refine current partition  $P$
- 4 Critical point found.

- Provable convergence in finite number of steps.

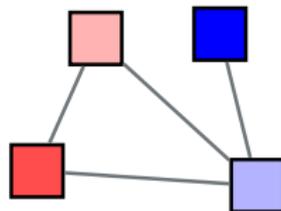
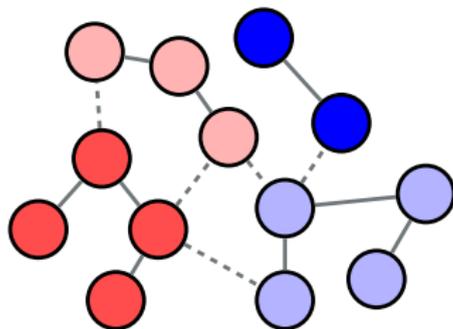


# Principle

---

- 1 Start with a trivial partition  
 $P = \{V\}$
- 2 Solve problem on reduced graph induced by  $P$
- 3 Refine current partition  $P$
- 4 Critical point found.

- Provable convergence in finite number of steps.
- In practice only a few iterations necessary.



## Refinement step

---

- **Objective:** add degrees of liberty to the reduced problem to decrease  $F$  as much as possible

## Refinement step

---

- **Objective:** add degrees of liberty to the reduced problem to decrease  $F$  as much as possible
- **Solution:** use first order information at current solution  $x$  to split along a step descent direction

$$\text{find } d^{(x)} \in \arg \min_{d \in D^V} F'(x, d) ,$$

## Refinement step

---

- **Objective:** add degrees of liberty to the reduced problem to decrease  $F$  as much as possible
- **Solution:** use first order information at current solution  $x$  to split along a step descent direction

$$\text{find } d^{(x)} \in \arg \min_{d \in D^V} F'(x, d) ,$$

with directional derivability:

$$F'(x, d) = \sum_{\substack{v \in V \\ d_v > 0}} \delta_v^+(x) - \sum_{\substack{v \in V \\ d_v < 0}} \delta_v^-(x) + \sum_{\substack{(u,v) \in E \\ x_u = x_v}} w_{(u,v)} |d_u - d_v| .$$

## Refinement step

- **Objective:** add degrees of liberty to the reduced problem to decrease  $F$  as much as possible
- **Solution:** use first order information at current solution  $x$  to split along a step descent direction

$$\text{find } d^{(x)} \in \arg \min_{d \in D^V} F'(x, d),$$

with directional derivability:

$$F'(x, d) = \sum_{\substack{v \in V \\ d_v > 0}} \delta_v^+(x) - \sum_{\substack{v \in V \\ d_v < 0}} \delta_v^-(x) + \sum_{\substack{(u,v) \in E \\ x_u = x_v}} w_{(u,v)} |d_u - d_v|.$$

- **In practice:** pick steepest direction in finite set  $D^V$ :

### Direction set:

smooth case ( $g_v = 0$  for all  $v \in V$ ):  $D = \{-1, +1\}$

nonsmooth case:  $D = \{-1, 0, +1\}$

Steepest direction as a graph cut problem.

## Implementation and variants

---

- Reduced problem: proximal algorithm (Preconditioned Forward Douglas-Rachford) on **reduced graph**

H. Raguét and L. Landrieu. Preconditioning of a Generalized Forward-Backward Splitting and Application to Optimization on Graphs. *SIAM Journal on Imaging Sciences*, 2015.

## Implementation and variants

---

- Reduced problem: proximal algorithm (Preconditioned Forward Douglas-Rachford) on **reduced graph**
- Refinement: graph cut on full graph with Boykov's augmenting path.

H. Raguét and L. Landrieu. Preconditioning of a Generalized Forward-Backward Splitting and Application to Optimization on Graphs. *SIAM Journal on Imaging Sciences*, 2015.

## Implementation and variants

---

- Reduced problem: proximal algorithm (Preconditioned Forward Douglas-Rachford) on **reduced graph**
- Refinement: graph cut on full graph with Boykov's augmenting path.
- Can be extended to multidimensional data (heuristic).

H. Raguét and L. Landrieu. Preconditioning of a Generalized Forward-Backward Splitting and Application to Optimization on Graphs. *SIAM Journal on Imaging Sciences*, 2015.

## Implementation and variants

---

- Reduced problem: proximal algorithm (Preconditioned Forward Douglas-Rachford) on **reduced graph**
- Refinement: graph cut on full graph with Boykov's augmenting path.
- Can be extended to multidimensional data (heuristic).
- Can be extended to the GMPP (heuristic).

H. Raguét and L. Landrieu. Preconditioning of a Generalized Forward-Backward Splitting and Application to Optimization on Graphs. *SIAM Journal on Imaging Sciences*, 2015.

## Implementation and variants

---

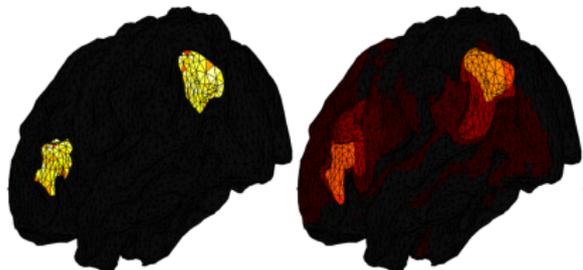
- Reduced problem: proximal algorithm (Preconditioned Forward Douglas-Rachford) on **reduced graph**
- Refinement: graph cut on full graph with Boykov's augmenting path.
- Can be extended to multidimensional data (heuristic).
- Can be extended to the GMPP (heuristic).
- Can be fully parallelized, even the graph cuts-based phase.

H. Raguet and L. Landrieu. Preconditioning of a Generalized Forward-Backward Splitting and Application to Optimization on Graphs. *SIAM Journal on Imaging Sciences*, 2015.

## EEG Experiment

---

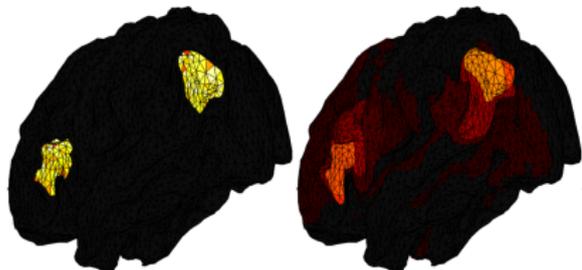
- EEG : from 96 electrods to  $\sim 20.000$  triangles



## EEG Experiment

---

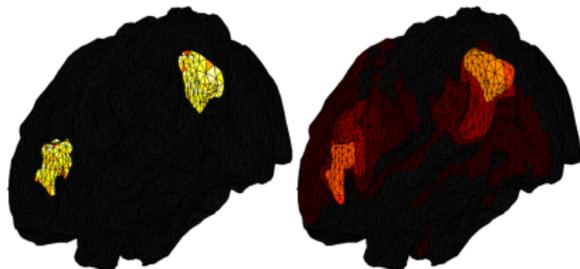
- EEG : from 96 electrodes to  $\sim 20,000$  triangles
- Underdetermined, ill-conditioned inverse problem



## EEG Experiment

---

- EEG : from 96 electrodes to  $\sim 20,000$  triangles
- Underdetermined, ill-conditioned inverse problem
- Sparsity, positivity, smoothness,

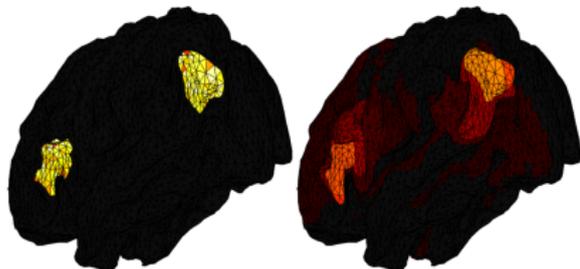


## EEG Experiment

---

- EEG : from 96 electrodes to  $\sim 20,000$  triangles
- Underdetermined, ill-conditioned inverse problem
- Sparsity, positivity, smoothness,

$$F : x \mapsto \frac{1}{2} \|y - \Phi x\|^2 + \sum_{v \in V} (\lambda_v |x_v| + \iota_{\mathbb{R}_+}(x_v)) + \sum_{(u,v) \in E} w_{(u,v)} |x_u - x_v| ,$$

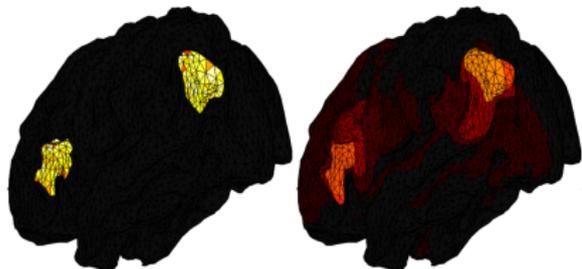


## EEG Experiment

---

- EEG : from 96 electrodes to  $\sim 20,000$  triangles
- Underdetermined, ill-conditioned inverse problem
- Sparsity, positivity, smoothness,
- Very coarse ground truth

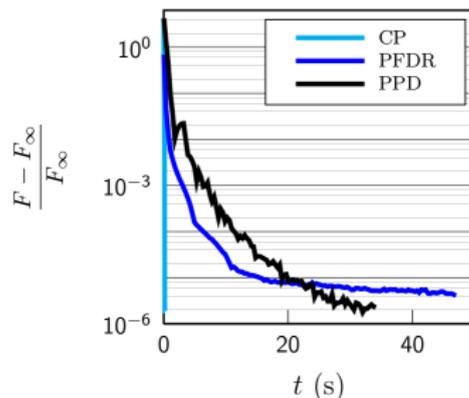
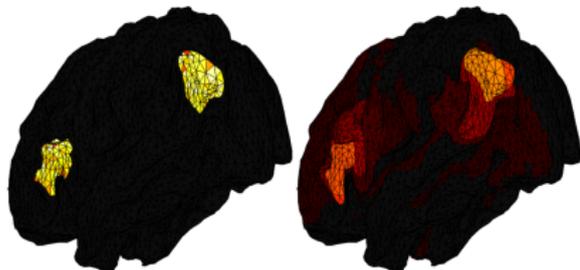
$$F : x \mapsto \frac{1}{2} \|y - \Phi x\|^2 + \sum_{v \in V} (\lambda_v |x_v| + \iota_{\mathbb{R}_+}(x_v)) + \sum_{(u,v) \in E} w_{(u,v)} |x_u - x_v|,$$



# EEG Experiment

- EEG : from 96 electrodes to  $\sim 20,000$  triangles
- Underdetermined, ill-conditioned inverse problem
- Sparsity, positivity, smoothness,
- Very coarse ground truth

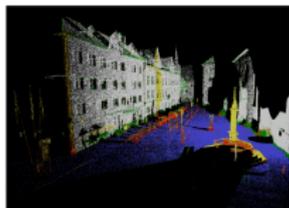
$$F : x \mapsto \frac{1}{2} \|y - \Phi x\|^2 + \sum_{v \in V} (\lambda_v |x_v| + \nu \mathbb{R}_+(x_v)) + \sum_{(u,v) \in E} w_{(u,v)} |x_u - x_v|,$$



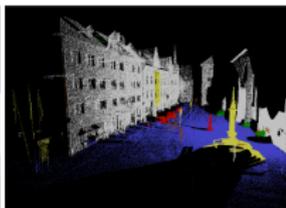
# Semantic Segmentation Experiment

---

- Spatial Regularization of pointwise probabilistic semantic segmentation  $q$  (from local context)



(b) Random forest predictions

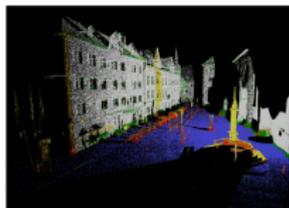


(c) Regularization

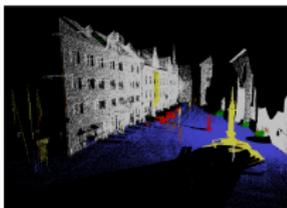
## Semantic Segmentation Experiment

---

- Spatial Regularization of pointwise probabilistic semantic segmentation  $q$  (from local context)
- A probability vector for each vertex



(b) Random forest predictions

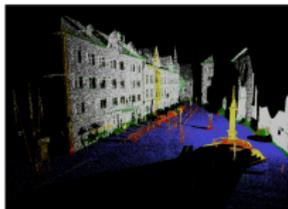


(c) Regularization

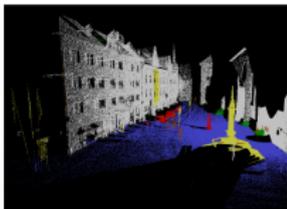
# Semantic Segmentation Experiment

---

- Spatial Regularization of pointwise probabilistic semantic segmentation  $q$  (from local context)
- A probability vector for each vertex
- KL-fidelity, simplex-bound, smoothness prior



(b) Random forest predictions

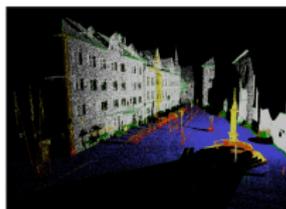


(c) Regularization

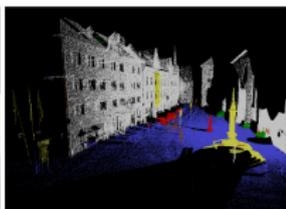
## Semantic Segmentation Experiment

- Spatial Regularization of pointwise probabilistic semantic segmentation  $q$  (from local context)
- A probability vector for each vertex
- KL-fidelity, simplex-bound, smoothness prior

$$F : p \mapsto \sum_{v \in V} \text{KL}(q_v, p_v) + \sum_{v \in V} \iota_{\Delta_K}(p_v) + \sum_{(u,v) \in E} w_{(u,v)} \|p_u - p_v\|_1,$$



(b) Random forest predictions

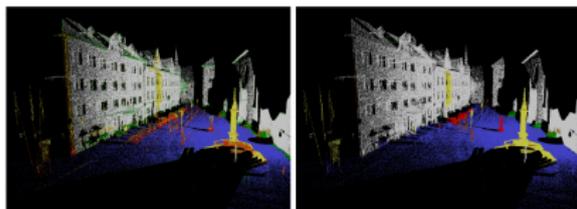


(c) Regularization

# Semantic Segmentation Experiment

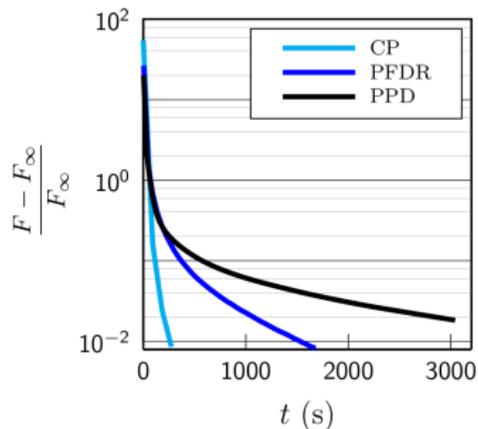
- Spatial Regularization of pointwise probabilistic semantic segmentation  $q$  (from local context)
- A probability vector for each vertex
- KL-fidelity, simplex-bound, smoothness prior

$$F : p \mapsto \sum_{v \in V} \text{KL}(q_v, p_v) + \sum_{v \in V} \iota_{\Delta_K}(p_v) + \sum_{(u,v) \in E} w_{(u,v)} \|p_u - p_v\|_1,$$



(b) Random forest predictions

(c) Regularization



# Presentation Layout

---

- 1 Deep Learning for 3D Point Clouds
- 2 Learning 3D Point Clouds Segmentation
- 3 The Cut Pursuit Algorithm
- 4 Conclusion**
- 5 Bibliography

## Conclusion

---

- Our paradigm for graph-structured learning and optimization:
  - Exploit the spatial regularity of the solution to increase speed and precision.

## Conclusion

---

- Our paradigm for graph-structured learning and optimization:
  - Exploit the spatial regularity of the solution to increase speed and precision.
  - Use neural networks to learn the inputs and parameters of efficient optimization algorithms.

## Conclusion

---

- Our paradigm for graph-structured learning and optimization:
  - Exploit the spatial regularity of the solution to increase speed and precision.
  - Use neural networks to learn the inputs and parameters of efficient optimization algorithms.
  - Use graph-structured optimization to compute the structure of neural network adapted to the data.

## Conclusion

---

- Our paradigm for graph-structured learning and optimization:
  - Exploit the spatial regularity of the solution to increase speed and precision.
  - Use neural networks to learn the inputs and parameters of efficient optimization algorithms.
  - Use graph-structured optimization to compute the structure of neural network adapted to the data.
- All our work is online:
  - 🔗 [loicland/superpoint-graph](#) 252 ★ 75 📄
  - 🔗 [loicland/cut-pursuit](#) 22 ★ 7 📄
  - 🔗 [1a7r0ch3/parallel-cut-pursuit](#) very soon!

# Presentation Layout

---

- 1 Deep Learning for 3D Point Clouds
- 2 Learning 3D Point Clouds Segmentation
- 3 The Cut Pursuit Algorithm
- 4 Conclusion
- 5 Bibliography**

## Bibliography I

---

**Qi et. al.2017a** Qi, C. R., Su, H., Mo, K., & Guibas, L. J. Pointnet: Deep learning on point sets for 3d classification and segmentation. CVPR, 2017

**Gaidon2016** Gaidon, A., Wang, Q., Cabon, Y., & Vig, E. Virtual worlds as proxy for multi-object tracking analysis. ,CVPR2016.

**Engelmann2017** Engelmann, F., Kontogianni, T., Hermans, A. & Leibe, B. Exploring spatial context for 3d semantic segmentation of point clouds. CVPR, DRMS Workshop, 2017.

**Hackel2017i** Timo Hackel and N. Savinov and L. Ladicky and Jan D. Wegner and K. Schindler and M. Pollefeys, SEMANTIC3D.NET: A new large-scale point cloud classification benchmark,ISPRS Annals of the Photogrammetry, Remote Sensing and Spatial Information Sciences,2017

**Armeni2016** Iro Armeni and Ozan Sener and Amir R. Zamir and Helen Jiang and Ioannis Brilakis and Martin Fischer and Silvio Savarese, 3D Semantic Parsing of Large-Scale Indoor Spaces, CVPR, 2016

**Demantke2011** Demantke, J., Mallet, C., David, N. & Vallet, B. Dimensionality based scale selection in 3D lidar point clouds. The International Archives of the Photogrammetry, Remote Sensing and Spatial Information Sciences, 2011.

**Weinmann2015** Weinmann, M., Jutzi, B., Hinz, S. & Mallet, C., Semantic point cloud interpretation based on optimal neighborhoods, relevant features and efficient classifiers. ISPRS Journal of Photogrammetry and Remote Sensing, 2015.

**Landrieu2017a** Landrieu, L., Raguét, H., Vallet, B., Mallet, C., & Weinmann, M. A structured regularization framework for spatially smoothing semantic labelings of 3D point clouds. ISPRS Journal of Photogrammetry and Remote Sensing, 2017.

## Bibliography II

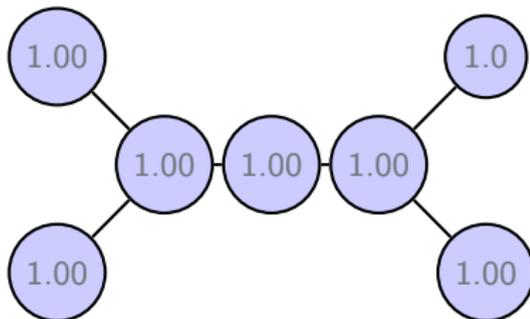
---

- Boulch2017** Boulch, Alexandre, Le Saux, Bertrand, and Audebert, Nicolas, Unstructured Point Cloud Semantic Labeling Using Deep Segmentation Networks, 3DOR, 2017.
- Wu2015** Wu, Z., Song, S. Khosla, A., Yu, F., Zhang, L., Tang, X., & Xiao, J. 3D shapenets: A deep representation for volumetric shapes. CVPR, 2015.
- Riegler2017** Riegler, G., Osman Ulusoy, A., & Geiger, A. Octnet: Learning deep 3d representations at high resolutions, CVPR, 2017.
- Tchapmi2017** Tchapmi, L., Choy, C., Armeni, I., Gwak, J. & Savarese, S., Segcloud: Semantic segmentation of 3d point clouds. 3DV, 2017.
- Jampani2018**, Jampani Su, H., , V. Sun, D., Maji, S., Kalogerakis, E., Yang, M. H., & Kautz, J., Splatnet: Sparse lattice networks for point cloud processing. CVPR2018.
- Tatarchenko2018** Tatarchenko, M., Park, J., Koltun, V., & Zhou, Q. Y. Tangent Convolutions for Dense Prediction in 3D. CVPR, 2018
- Li2018** Li, Y., Bu, R., Sun, M., Wu, W., Di, X., & Chen, B. PointCNN: Convolution On  $\chi$ -Transformed Points. NIPS, 2018.
- Qi2017** Qi, X., Liao, R., Jia, J., Fidler, S., & Urtasun, R. 3D Graph Neural Networks for RGBD Semantic Segmentation. In PCVPR, 2017.
- Simonovsky2017** Simonovsky, M., & Komodakis, N. Dynamic edge-conditioned filters in convolutional neural networks on graphs. CVPR, 2017.
- Landrieu&Simonovski2018** Landrieu, L., & Simonovsky, M. Large-scale point cloud semantic segmentation with superpoint graphs. CVPR, 2018
- Qi et. al.2017b** Qi, C. R., Yi, L., Su, H., & Guibas, L. J. (2017). Pointnet++: Deep hierarchical feature learning on point sets in a metric space. In Advances in Neural Information Processing Systems (pp. 5099-5108).

## Non-differentiability of the naive pipeline

---

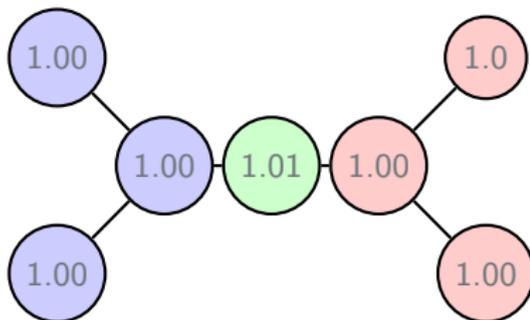
- Non differentiability of the CCC operator



## Non-differentiability of the naive pipeline

---

- Non differentiability of the CCC operator
- ⇒ Tiny changes - large consequence



## Non-differentiability of the naive pipeline

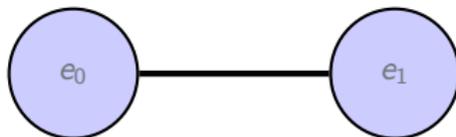
---

- Non differentiability of the CCC operator

$$f^* = \arg \min \|f_0 - e_0\|^2 + \|x_1 - e_1\|^2 + 0.5[f_0 \neq f_1]$$

⇒ Tiny changes - large consequence

- Non differentiability of  $f^*(e)$

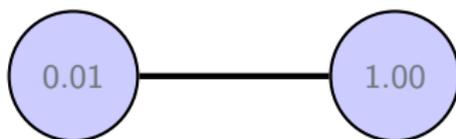


## Non-differentiability of the naive pipeline

---

$$f^* = \arg \min \|f_0 - e_0\|^2 + \|x_1 - e_1\|^2 + 0.5[f_0 \neq f_1]$$

- Non differentiability of the CCC operator
- ▬ Tiny changes - large consequence
- Non differentiability of  $f^*(e)$



$$f_0^* = 0.505, \quad f_1^* = 0.505$$

## Non-differentiability of the naive pipeline

---

$$f^* = \arg \min \|f_0 - e_0\|^2 + \|x_1 - e_1\|^2 + 0.5[f_0 \neq f_1]$$

- Non differentiability of the CCC operator
- = Tiny changes - large consequence
- Non differentiability of  $f^*(e)$
- = non-continuous w.r.t inputs



$$f_1^* = -0.01, \quad f_1^* = 1.00$$